## M.Sc. Mathematics

| SEM | Course Code | Course | Course Title | Ins. <br> Hrs / <br> Week | Credit | $\begin{gathered} \text { Exam } \\ \text { Hrs } \end{gathered}$ | Marks |  | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | CIA | ESE |  |
| I | 20PMA1CC1 | Core-I | Algebra-I | 6 | 5 | 3 | 25 | 75 | 100 |
|  | 20PMA1CC2 | Core - II | Real Analysis | 6 | 5 | 3 | 25 | 75 | 100 |
|  | 20PMA1CC3 | Core- III | Classical Dynamics | 6 | 4 | 3 | 25 | 75 | 100 |
|  | 20PMA1CC4 | Core - IV | Ordinary Differential Equations | 6 | 4 | 3 | 25 | 75 | 100 |
|  | 20PMA1DE1 | DSE-I \# |  | 6 | 4 | 3 | 25 | 75 | 100 |
|  |  |  | TOTAL | 30 | 22 |  |  |  | 500 |
| II | 20PMA2CC5 | Core - V | Algebra-II | 6 | 5 | 3 | 25 | 75 | 100 |
|  | 20PMA2CC6 | Core - VI | Complex Analysis | 6 | 5 | 3 | 25 | 75 | 100 |
|  | 20PMA2CC7 | Core- VII | Topology | 6 | 4 | 3 | 25 | 75 | 100 |
|  | 20PMA2CC8 | Core - VIII | Numerical Analysis | 6 | 4 | 3 | 25 | 75 | 100 |
|  | 20PMA2DE2 | DSE - II \# |  | 6 | 4 | 3 | 25 | 75 | 100 |
|  |  |  | TOTAL | 30 | 22 |  |  |  | 500 |
| III | 20PMA3CC9 | Core- IX | Functional Analysis | 6 | 5 | 3 | 25 | 75 | 100 |
|  | 20PMA3CC10 | Core- X | Partial Differential Equations | 6 | 5 | 3 | 25 | 75 | 100 |
|  | 20PMA3CC11 | Core- XI | Modern Probability Theory | 6 | 4 | 3 | 25 | 75 | 100 |
|  | 20PMA3CC12 | Core- XII | Advanced Graph Theory | 6 | 4 | 3 | 25 | 75 | 100 |
|  | 20PMA3DE3T | DSE - III (a)\# |  | 3 | 2 | 3 | 10 | 40 | 50 |
|  | 20PMA3DE3P | DSE - III (b)\# |  | 3 | 2 | 3 | 10 | 40 | 50 |
|  | 20PMA3EC1 | Extra Credit Course I | Online Course (MOOC) | - | 1* | - | - | - | - |
|  |  |  | TOTAL | 30 | 22 |  |  |  | 500 |
| IV | 20PMA4CC13 | Core- XIII | Measure theory and integration | 6 | 5 | 3 | 25 | 75 | 100 |
|  | 20PMA4CC14 | Core- XIV | Fluid Dynamics | 6 | 5 | 3 | 25 | 75 | 100 |
|  | 20PMA4CC15 | Core-XV | Integral Equations and Calculus of Variations | 6 | 5 | 3 | 25 | 75 | 100 |
|  | 20PMA3DE4 | DSE - IV \# |  | 6 | 4 | 3 | 25 | 75 | 100 |
|  | 20PMA4PW | Project | Internship and Project Report | 6 | 4 | - | - | 100 | 100 |
|  | 20PCNOC | Online Course (Compulsory) |  | - | 1 | - | - | - | - |
|  | 20PMA4EC2 | Extra Credit Course II | Mathematics for career examinations | - | 5* | 3 | - | 100 | 100* |
|  |  |  | TOTAL | 30 | 24 |  |  |  | 500 |
| GRAND TOTAL |  |  |  |  | 90 |  |  |  | 2000 |

*Not considered for grand total and CGPA
\# Discipline Specific Electives

| SEMESTER | Course Code | DISCIPLINE SPECIFIC ELECTIVE |
| :---: | :--- | :--- |
| I | 20PMA1DE1A | Mathematics of Finance |
|  | 20PMA1DE1B | Control Theory |
|  | 20PMA2DE2A | Fuzzy Analysis \& its Applications |
|  | 20PMA2DE2B | Mathematical Methods in Biology |
| III | 20PMA3DE3AT | Python Programming |
|  | 20PMA3DE3AP | Python Programming - Practical |
|  | 20PMA3DE3B | Computer Algorithms |
| IV | 20PMA4DE4A | Advanced Operations Research |
|  | 20PMA4DE4B | Stochastic Processes |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | 20PMA1CC1 | Core - I | ALGEBRA-I | 6 | 5 | 100 | 25 | $\mathbf{7 5}$ |

## Course Outcomes:

At the end of the Course, Students will be able to:

1. Discuss Sylow's theorems, Solvability of Symmetric group with examples.
2. Construct new groups from existing groups using direct products and illustrate withsome examples.
3. Recognize the concept of vector spaces as R -module.
4.Describe some of the canonical forms of linear transformations such as triangular andnilpotent transformations.
4. Solve problems based on different kinds of transformations.

## Unit I

18hours
Another Counting Principle - Sylow's Theorems (for Theorem 2.12.1, first proof only).

## Unit II <br> 18 hours

Solvability by Radicals - \#Direct Products\# - Finite Abelian Groups - Modules.

## Unit III

18 hours
Canonical Forms: Triangular Form - Nilpotent Transformations.

## Unit IV

18 hours
Canonical Forms: Jordan Form - Rational Canonical Form.

## Unit V

18 hours
\#Trace and Transpose\# - Hermitian, Unitary and Normal Transformations - Real Quadratic Forms.
\# \# Self-study portion.

## Text Book:

I. N. Herstein, Topics in Algebra, Second Edition, Wiley India Pvt. Ltd., New Delhi, 2006

| UNIT I | Chapter 2: Sections 2.11, 2.12 (Section 2.12: Omit Lemma 2.12.5) |
| :--- | :--- |
| UNIT II | Chapter 5: Section 5.7 (Lemma 5.7.1, Lemma 5.7.2, Theorem 5.7.1 only) <br>  <br>  <br>  <br> Chapter 2: Sections 2.13, 2.14 (Section 2.14: Theorem 2.14.1 only) <br> Chapter 4: Section 4.5 |
| UNIT III | Chapter 6: Sections 6.4, 6.5 |
| UNIT IV | Chapter 6: Sections 6.6, 6.7 |
| UNIT V | Chapter 6: Sections 6.8, 6.10, 6.11 |

## Books for Reference:

1. P.B. Bhattacharya, S.K. Jain and S.R. Nagpaul, Basic Abstract Algebra, Second Edition, Cambridge University Press , (1995).
2. Michael Artin, Algebra, Second edition, Pearson-Prentice Hall, New Delhi, 2015
3. Vijay K Khanna and S K Bhambri, A course in Abstract Algebra, Third Edition, Vikas Publishing House Pvt. Ltd.
Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 20PMA1CC1 |  |  | ALGEBRA-I |  |  |  | 6 | 5 |  |
| Course Outcomes | Programme Outcomes(POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO2 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO3 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO4 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO5 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| Number of Matches= 42, Relationship : HIGH |  |  |  |  |  |  |  |  |  |  |

Prepared by:
Mr. N. Mohamed Thoiyab
Ms. B.ShafinaBanu
Ms. C.Vijayalakshmi

Checked by:
Dr.A. Solairaju

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | 20PMA1CC2 | Core - II | REAL ANALYSIS | 6 | 5 | $\mathbf{1 0 0}$ | $\mathbf{2 5}$ | $\mathbf{7 5}$ |

## Course Outcome:

At the end of the Course, Students will be able to:

1. Discuss the basic concepts of topology and illustrate with examples.
2. Apply domain knowledge for Riemann - Stieltjes integral.
3. Explain the sequences and series of functions with the examples.
4.Determine the partial derivatives and directional derivatives.
4. Prove the chain rule, inverse function theorem and Implicit function theorem.

## UNIT I <br> 18 hours

Basic topology - Metric spaces - Compact sets - Perfect sets.

## UNIT II

18 hours
Riemann - Stieltjes integral - Definition and existence of the integral - \#Properties of the integral\# - Integration and differentiation - Rectifiable Curves.

## UNIT III

18 hours
Sequences and series of functions - Uniform convergence- Uniform convergence and continuity - Uniform convergence and integration - Uniform convergence and differentiation - Stone -Weierstrass theorem.

## UNIT IV

18 hours
Multivariable differential calculus - Directional derivatives - Total derivative - Matrix of linear function - Jacobian matrix - Chain rule - Mean value theorem - Sufficient condition for differentiability- Equality of partial derivatives - Taylor's formula.

## UNIT V

18 hours
Functions with non-zero Jacobian determinant - Inverse function theorem - Implicit function theorem.

## \# \# Self-study portion.

## Text Books:

T.B-1. Walter Rudin, Principles of Mathematical Analysis, McGraw-Hill International

Editions, Third
Edition (1987).
T.B-2. Tom M. Apostol, Mathematical Analysis, Addison-Wesley Publishing Company, Second Edition
(1974).

| UNIT I | Chapter 2 | Sections 2.15-2.43 | T.B-1 |
| :--- | :--- | :--- | :--- |
| UNIT II | Chapter 6 | Sections 6.1-6.22, 6.26, 6.27 | T.B-1 |
| UNIT III | Chapter 7 | Sections 7.1-7.18,7.26, 7.27 | T.B-1 |
| UNIT IV | Chapter 12 |  | T.B-2 |
| UNIT V | Chapter 13 | Sections 13.1-13.4 | T.B-2 |

## Books for Reference:

1. V. Ganapathy Iyer, Mathematical analysis, Tata McGraw-Hill Publishing Company, Ltd,
(1977).
2. Gabriel Klambauer, Real Analysis, American Elsevier Publishing Company, INC, (1973). Web Source
https://nptel.ac.in/courses/111/106/111106053/ https://nptel.ac.in/courses/111/105/111105069/ https://nptel.ac.in/courses/111/105/111105098/

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 20PMA1CC2 |  |  | REAL ANALYSIS |  |  |  | 6 | 5 |  |
| Course Outcomes | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO2 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  |
| CO3 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO4 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  |
| CO5 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| Number of Matches= 36, Relationship : HIGH |  |  |  |  |  |  |  |  |  |  |

## Prepared by :

Mr. S. Masoothu
Dr. D. Dhamodharan

## Checked by :

Mr.N.Mohamed Thoyaib

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | 20PMA1CC3 | Core - III | CLASSICAL <br> DYNAMICS | 6 | 4 | 100 | 25 | 75 |

## Course Outcomes

At the end of the Course, Students will be able to:

1. Discuss the basic concepts of Mechanical System.
2. Derivation of Lagrange's Equation for holonomic and non holonomic system and solve simple problems.
3. Analyze the applications of Impulsive Motion.
4. Examine the concept of Hamilton's principle and other variational principles.
5. Express the ideas of separability using Stackle's Theorem and solving problems.

## Unit I

18 hours
Mechanical system - Generalized Co-ordinates - Constraints - Virtual work - \#Energy and Momentum\#

## Unit II

Derivation of Lagrange's Equation - Examples - Integrals of the motion - Simple Problems

## Unit III

18 hours
Rayleigh's Dissipation Function - Impulsive motion - \#Velocity dependent potentials\#

## Unit IV

18 hours
Hamilton`s principle - Hamilton's equation - \#Other variational principles\#

## Unit V

18 hours
Hamilton`s principal function - The Hamilton's - Jacobi equation - Separability- Simple Problems
\# \#Self-study portion.

## Text Book

Donald. T. Green wood, Classical Dynamics, Prentice Hall of India, (1985).

| UNIT I | Sections $1.1-1.5$ |
| :--- | :--- |
| UNIT II | Sections $2.1-2.3$ |
| UNIT III | Sections 3.1, 3.2 and 3.4 |
| UNIT IV | Sections 4.1, 4.2, 4.3 |
| UNIT V | Sections 5.1, 5.2 and 5.3 |

## Books for Reference

C.R. Mondal, Classical Mechanics, Revised Edition, Prentice Hall of India, (2008).

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 20PMA1CC3 |  |  | CLASSICAL DYNAMICS |  |  |  | 6 | 4 |  |
|  | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  |
| CO2 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ |
| CO3 | $\checkmark$ |  |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO4 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| CO5 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| Number of Matches= 36, Relationship : HIGH |  |  |  |  |  |  |  |  |  |  |

Prepared by:
N. Abdul Ali
M.S. Afya Farhana

Checked by:
Dr.S.Mohamed Yusuff Ansari

| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | 20PMA1CC4 | Core - IV | ORDINARY <br> DIFFERENTIAL <br> EQUATIONS | 6 | 4 | 100 | 25 | 75 |

## Course Outcomes:

At the end of the Course, Students will be able to:

1. Apply domain knowledge for solving second order linear differential equations and method of variation of parameters.
2. Demonstrate and discuss Oscillations, Sturm separation and comparison Theorem with examples.
3. Show regular singular points and solve Gauss's Hyper geometric equation with examples.
4. Investigate Legendre polynomials and Bessel functions with examples.
5. Determine linear systems with illustrative examples and Prove Picard's theorem.

## UNIT I

18 hours
Second order linear Equations- \#The general solution of the Homogeneous equation\# The Use of a known solution to find another- The Homogeneous equation with constant coefficients-The method of variation of parameters.

## UNIT II

18 hours
Oscillations and the Sturm separation theorem - The Sturm comparison theorem Series solutions of First order equations-Second order linear equations-ordinary points. UNIT III

18 hours
Regular singular points-Regular singular points (continued) - Gauss's Hypergeometric equation-\# The point at Infinity\#.

## UNIT IV

18 hours
Legendre Polynomials - Properties of Legendre Polynomials - Bessel functions -\#The Gamma function\#-Properties of Bessel functions.

## UNIT V

18 hours
Linear systems- Homogeneous linear systems with constant coefficients - The method of successive approximations -Picard's theorem.

## \# \# Self-study portion.

## Text Book:

G.F.Simmons, Differential Equations with Applications and Historical notes, second edition, Tata McGraw-Hill Publishing company Ltd, New Delhi, 2003.
UNIT I Sections 14, 15, 16, 17,19
UNIT II Sections 24, 25, 27, 28
UNIT III Sections 29, 30, 31, 32
UNIT IV Sections 44, 45, 46, 47
UNIT V Sections 55, 56, 68, 69

## Books for Reference:

1. Earl .A. Coddington, An Introduction to Ordinary Differential equations, PHI, 1961.
2. M.D. Raisinghania, Advanced Differential Equations, Seventh Revised Edition, S. Chand and Company Ltd, New Delhi, 2000.

Website and e-learning source
https://nptel.ac.in/courses/111/106/111106100/
https://nptel.ac.in/courses/111/108/111108081/
https://nptel.ac.in/courses/111/107/111107111/

## Unit-I

Introduction to Second order ODE's
(https://www.youtube.com/watch?time continue=2\&v=dPJYOi5qNzU)
Properties of solutions of second order homogeneous ODE
(https://www.youtube.com/watch?v=iQ6SN5CDKTw)
The Use of a known solution to find another (https://www.youtube.com/watch?time continue=1\&v=U5s1z9qaZng), (https://www.youtube.com/watch?v=C3C67IXZIgQ)

The Homogeneous equation with constant coefficients
(https://www.youtube.com/watch?v=IUpQg32D9kE),
(https://www.youtube.com/watch?v=NvXF62IIICY)
The method of variation of parameters (https://www.youtube.com/watch?v=b|F7FUu9Vtk)

## Unit-II

ordinary points (https://www.youtube.com/watch?time continue=1585\&v=E9Mx1Ef cDO)
Second order linear equations (https://www.youtube.com/watch?v=utSvQMsr3g8), (https://www.youtube.com/watch?time continue=2037\&v=YQcFBh6HQ9o)

## Unit-III

Legendre differential equation
(https://www.youtube.com/watch?time continue=2\&v=5c4KptxCS80)
Power series solutions around a regular singular point
(https://www.youtube.com/watch?time continue=1944\&v=3mKFtZl6ZZs)
Frobenius method (https://www.youtube.com/watch?v=2LdCV3qf-ZI),
(https://www.youtube.com/watch?v=FOlHg93WtjY),
(https://www.youtube.com/watch?time continue=1\&v=KcTgFeyJ6h0)

## Unit-IV

Legendre polynomials (https://www.youtube.com/watch?v=k5n698fUwuU)
Properties of Legendre Polynomials (https://www.youtube.com/watch?v=g2BifBEjmnM)

## Bessel differential equation (https://www.youtube.com/watch?v= UmpTFoKqxE)

The Gamma function (https://www.youtube.com/watch?v=aK61gh-wUa4)
Properties of Bessel functions (https://www.youtube.com/watch?v=8KIs9zzTS8c),
(https://www.youtube.com/watch?time continue=4\&v=MvZecjM4at8)

## Unit-V

Pichard's Theorem
(https://www.youtube.com/watch?v=oL97oGZUINA\&list=PLbMVogVj5nJSGlf9sluucwobyr z z6gID\&index=19\&t=0s),
(https://www.youtube.com/watch?v=2DalNaf1Zfo\&list=PLbMVogVj5nJSGlf9sluucwobyr zz6 g|D\&index=20\&t=0s)

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 20PMA1CC4 |  |  | ORDINARYDIFFERENTIALEQUATIONS |  |  |  | 6 |  | 4 |
| Course Outcomes (COs) | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| CO2 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| CO3 | $\checkmark$ |  |  | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ |
| CO4 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ | $\checkmark$ |  |
| CO5 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| Number of Matches= 34, Relationship : Moderate |  |  |  |  |  |  |  |  |  |  |

Prepared by :
Dr. S. Ismail Mohideen
Dr. M.A. Rifayathali
Dr. K.S. Kanzul Fathima

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | 20PMA1DE1A | DSE - I | MATHEMATICS <br> OF FINANCE | 6 | 4 | 100 | 25 | 75 |

## Course Outcomes:

At the end of the Course, Students will be able to:
1.Recall basic concepts of simple interest, simple discount, equivalent rates and discount value
2.Expain an accumulated and discount values for fractional interest period.
3.Apply the mathematical idea of annuities with examples.
4.Analyze the Amortization of a debit.
5.Bring out bounds and related properties with illustrations.

## UNIT I

18 hours
Simple interest- \#time between dates- equation of value- partial payments- simple discount- promissory notes\#. Compound interest- accumulated values- compound interest tables- present values- nominal and effective rates of interest- discount and discounted values.

## UNIT II

## 18 hours

Compound interest- Varying rates of interest-equation of values- equated time payment. Annuities certain- present values-accumulated values- Annuity due- present valuesaccumulated values- deferred annuity certain- present values- accumulated values- deferred annuity due- present values- accumulated values.

## UNIT III

## 18 hours

Perpetuity - immediate certain perpetuity-present values- accumulated valuesimmediate perpetuity due- present values- accumulated values- deferred perpetuity-present values- accumulated values- variable annuities- increasing annuities- successive instalments form an AP- successive instalments form a GP- Annuities with frequency different from that with interest is convertible.

## UNIT IV

## 18 hours

Redemption of loan- amortization of a debt- outstanding principal- interest portion \& principal content in a particular repayment- Redemption of a loan by a sinking fund Lender's sinking - further consideration on redemption of loan- Capital redemption policypure premiums - office premium

Further compound interest and investment yields-nominal and effective rates of discount- relation between $\mathrm{i}(\mathrm{m})$ and $\mathrm{d}(\mathrm{m})$ - the average yield on the life fund- weighted rate of return-money weighted rate of return- time weighted rate of return- linked internal rate of return. Bonds- purchase price-callable bonds- premium and discount-other types of bonds

## \# \#Self-study portion.

## Text Books:

1. Foundation of Actuarial Science (IC-28), Study Material Published by Insurance Institute of India, Mumbai, Reprinting February 2017.
2. Mathematics of Finance, Second edition (2005), Peter Zima and Robert L.Brown,Tata McGraw-Hill Publishing Company Limited, New Delhi.

| Unit I | Chapter 3 Section 3.1 to 3.6 | T.B2 |
| :--- | :--- | :--- |
|  | Chapter 1 Section 1 to 7 | T.B1 |
| Unit II | Chapter 1 Section 8 to 10 | T.B1 |
|  | Chapter 2 Section 1 to 13 | T.B1 |
| Unit III | Chapter 2 Section 14 \&15 | T.B1 |
|  | Chapter 3 Section 1 to 5 | T.B1 |
| Unit IV | Chapter 4 Section 1 to 8 | T.B1 |
| Unit V | Chapter 5 Section 1 to 6 | T.B1 |
|  | Chapter 8 Section 8.1 to 8.7 | T.B2 |

## Books for Reference:

An introduction to the Mathematics of Finance, MC Cutchoon and Scoot-Hoinenmann Professional Publishing.

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 20PMA1DE1A |  |  | MATHEMATICS OFFINANCE |  |  |  | 6 | 4 |  |
| Course Outcomes | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 |
| CO1 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO2 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| CO3 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  |  | $\checkmark$ | $\checkmark$ |  |
| CO4 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO5 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| Number of Matches= 38, Relationship : HIGH |  |  |  |  |  |  |  |  |  |  |

## Prepared by:

Dr.A.Prasanna
A.Nafiunisha

## Checked by:

Dr.M.Mohamed Althaf

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | 20PMA1DE1B | DSE - I | CONTROL <br> THEORY | 6 | 4 | 100 | 25 | 75 |

## Course Outcome:

At the end of the Course, Students will be able to:

1. Discuss the basic concepts of Observability and illustrate the examples.
2. Explain controllability and nonlinear systems with the examples.
3. Apply the domain knowledge of asymptotic stability of linear systems and perturbed linear systems.
4. Analyze the stabilization via linear feedback control.
5. Solve the matrix Riccati equations

## UNIT I <br> 18 hours

Observability: Linear Systems - Observability Grammian- Constant coefficient system Reconstruction kernel - Nonlinear Systems

## UNIT II

18 hours
Controllability: Linear systems - Controllability Grammian - Adjoint systems - Constant coefficient systems - steering function - Nonlinear systems

UNIT III
18 hours
Stability:Stability - Uniform Stability - Asymptotic Stability of Linear Systems - Linear time varying systems - Perturbed linear systems - Nonlinear systems

## UNIT IV

18 hours
Stabilizability: Stabilization via linear feedback control - Bass method - Controllable subspace Stabilization with restricted feedback

## UNIT V

18 hours
Optimal control: Linear time varying systems with quadratic performance criteria - Matrix Riccati equation - Linear time invariant systems - Nonlinear Systems

## Text Book:

Elements of Control Theory by K.Balachandran and J.P.Dauer, Narosa, New Delhi, 1999.

| UNIT I | Chapter 2 |
| :--- | :--- |
| UNIT II | Chapter 3 |
| Sections 3.1-3.3 |  |
| UNIT III | Chapter 4 |
| UNIT IV | Chapter 5 |
| UNIT V | Chapter 6 |

## Books for Reference:

1. Linear Differential Equations and Control by R.Conti, Academic Press,London, 1976.
2. Functional Analysis and Modern Applied Mathematics by R.F.CurtainandA.J.Pritchard, Academic Press, New York, 1977.
3. Controllability of Dynamical Systems by J.Klamka, Kluwer AcademicPublisher, Dordrecht, 1991.
4. Mathematics of Finite Dimensional Control Systems by D.L.Russell, MarceIDekker, New York,1979.
5. E.B. Lee and L. Markus, Foundations of optimal Control Theory, John Wiley,New York, 1967

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 20PMA1DE1B |  |  | CONTROL THEORY |  |  |  | 6 | 4 |  |
| Course Outcomes | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO2 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  |
| CO3 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO4 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  |
| CO5 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| Number of Matches= 36, Relationship : HIGH |  |  |  |  |  |  |  |  |  |  |

## Prepared by :

## Checked by :

Dr.A.Prasanna
Dr.M.A.Rifayath Ali

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| II | 20PMA2CC5 | Core - V | ALGEBRA-II | 6 | 5 | 100 | 25 | $\mathbf{7 5}$ |

## Course Outcomes

At the end of the Course, Students will be able to:

1. Discuss the algebraic concepts of finite and infinite fields and its illustrations.
2. Analyze the fundamental concepts of algebra and their role in modern mathematics.
3. Recognize and Recall the algebraic expressions, using the commutative, associative and distributive properties.
4. Explain the accurate and efficient use of advanced algebraic techniques
5. Demonstrate mathematical ideas through analyzing, proving and explaining concepts from advanced algebra

## Unit I

## 18 hours

Extension fields - The Transcendence of $e$.

## Unit II

18 hours
Roots of Polynomials - More about Roots.

## Unit III

18 hours
The Elements of Galois Theory.

## Unit IV

18 hours
Finite Fields - Wedderburn's Theorem on Finite Division Rings.

## Unit V

18 hours
Solvability by Radicals - A Theorem of Frobenius - Integral Quaternions and the FourSquare Theorem.

## Text Book

I. N. Herstein, Topics in Algebra, Second Edition, Wiley India Pvt. Ltd., New Delhi,2006.

UNIT I Chapter 5 Sections 5.1, 5.2
UNIT II Chapter5 Sections 5.3, 5.5
UNIT III Chapter 5 Section 5.6
UNIT IV Chapter 7 Sections 7.1, 7.2 (Theorem 7.2.1 only)
UNIT V Chapter 5 Section 5.7(Omit Lemma 5.7.1 Lemma 5.7.2 and Theorem 5.7.1). Chapter 7 Sections 7.3, 7.4

## Books for Reference

1. M. Artin, Algebra, Pearson - Prentice Hall, New Delhi,2007
2. P.B. Bhattacharya, S.K. Jain and S.R. Nagpaul, Basic Abstract Algebra, Second (Indian) Edition, Cambridge University Press,1997

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 20PMA2CC5 |  |  | ALGEBRA-II |  |  |  | 6 | 5 |  |
| CourseOutcomes (COs) | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| CO2 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO3 | $\checkmark$ |  |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| CO4 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |  | $\checkmark$ | $\checkmark$ |
| CO5 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| Number of Matches= 39, Relationship : HIGH |  |  |  |  |  |  |  |  |  |  |

Prepared by:
Dr. A.Solai Raju
Mr. N. Mohamed Thoiyab
Checked by:

Dr. D.Dhamodaran
Ms. A. FathimaBegam

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| II | 20PMA2CC6 | Core - VI | COMPLEX <br> ANALYSIS | 6 | 5 | 100 | 25 | 75 |

## Course Outcome:

At the end of the Course, Students will be able to:

1. Recognize the basic concept of Line integrals, rectifiable arcs with examples and prove Cauchy's theorems.
2. Demonstrate the homology in complex plain and prove Taylor's theorem.
3. Discuss argument principle and evaluate the definite integrals.
4. Describe the properties of Harmonic functions and prove Poisson's formula.
5. Explain the canonical products and gamma functions with examples.

## UNIT I

18 hours
Fundamental theorems - Line integrals - Rectifiable arcs - Line integrals as functions of arcs -Cauchy's theorem for a rectangle - Cauchy's theorem in a disk. Cauchy's integral formula Index of a point with respect to a closed curve - Integral formula for higher derivatives.

## UNIT II

18 hours
Local properties of analytical functions - Removable singularities - Taylor's theorem - Zeros and poles. Local mapping - Maximum principle. General form of Cauchy theorem - Chains and cycles -Simple connectivity - Homology.

## UNIT III

## 18 hours

General statement of Cauchy's theorem - Proof of Cauchy's theorem - Locally exact differentials. Calculus of residue - Residue theorem - Argument principle - Evaluation of definite integrals.

## UNIT IV

## 18 hours

Harmonic functions - Definition and basic properties - Mean-value property - Poisson's formula- Schwartz's theorem - Reflection principle. Power series expansions - Weierstrass's theorem - Taylor series - Laurent series.

UNIT V
18 hours
Partial fractions and factorization - Partial fractions - Infinite products - Canonical products Gamma functions.

## Text Book:

Lars. V. Ahlfors, Complex Analysis, McGraw Hill International Edition, Third Edition (1979).

UNIT I Chapter 4 Sections 1.1-1.5, 2.1-2.3.
UNIT II Chapter 4 Sections 3.1-3.4, 4.1-4.3.
UNIT III Chapter 4 Sections 4.4-4.6, 5.1-5.3
UNIT IV Chapter 4 Sections 6.1-6.5
Chapter 5 Sections 1.1-1.3
UNIT V Chapter 5 Sections 2.1-2.4

## Books for Reference:

1. Jacob Sonnenschein and Simon Green, Elements of Complex analysis, Dickenson Publishing Company, INC. (1977).
2. S. Ponnusamy, Foundations of Complex Analysis, NarosaPvt. Ltd., Second Edition (2008).

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours | Credits |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| II | 20PMA2CC6 |  |  | COMPLEX ANALYSIS |  |  |  | 6 | 5 |  |
|  | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO2 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO3 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ |  |  |
| CO4 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO5 | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| Number of Matches= 38, Relationship : HIGH |  |  |  |  |  |  |  |  |  |  |

Prepared by :
Dr.R.Jahir Hussain

Checked by :
Dr.A.Mohamed Ismayil

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| II | 20PMA2CC7 | Core - VII | TOPOLOGY | 6 | $\mathbf{4}$ | $\mathbf{1 0 0}$ | $\mathbf{2 5}$ | $\mathbf{7 5}$ |

## Course Outcome:

At the end of the Course, Students will be able to:

1. Illustrate and Describe the origin of topological spaces.
2. Apply domain knowledge for metric space and connected spaces with examples.
3. Prove the Tychonoff theorem with examples.
4.Determine the countability axioms, separation axioms and prove the Urysohn lemma.
4. Explain the Baire category theorem in topological point of view.

## UNIT I

## 18 hours

Topological spaces - Basis for a topology- Order topology, product topology- Subspace Topology - Closed sets and limit points - Continuous functions - \# Product Topology \#.

## UNIT II

18 hours
Metric topology - Metric topology (continued) - Connected spaces.

## UNIT III

18 hours
Compact spaces - Limit point compactness - Tychonoff theorem.

## UNIT IV

## 18 hours

Countability axioms - Separation axioms - Urysohn lemma - Urysohnmetrization theorem Completely regular spaces.

## UNIT V

18 hours
Complete metric spaces - Compactness in metric spaces - Baire spaces.

## \# \# Self-study portion.

## Text Book:

James R. Munkres, Topology A First Course, Prentice Hall of India, (1998).

UNIT I Sections 2.1-2.8
UNIT II Sections 2.9, 2.10, 3.1
UNIT III Sections 3.5, 3.7, 5.1
UNIT IV Sections 4.1-4.4, 5.2
UNIT V Sections 7.1, 7.3, 7.7

## Books for Reference:

1. Sze-Tsen Hu, Elements of General Topology, Holden Day, INC. (1964).
2. K.D. Joshi, Introduction to General Topology, Wiley Eastern Ltd. (1983).

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours | Credits |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| II | 20PMA2CC7 |  |  | TOPOLOGY |  |  |  | 6 | 4 |  |
|  | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO2 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO3 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |
| CO4 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| CO5 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| Number of Matches= 38, Relationship : HIGH |  |  |  |  |  |  |  |  |  |  |

Prepared by :
Dr. A. Nagoor Gani

Checked by :
Dr.M.Mohammed Jabarulla

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| II | 20PMA2CC8 | Core-VIII | NUMERICAL <br> ANALYSIS | 6 | 4 | 100 | 25 | 75 |

## Course Outcomes:

At the end of the Course, Students will be able to:

1. Recall the iteration methods to solve the problems.
2. Identify the approximate solution to the given problems.
3. Find the interpolation value with illustrations.
4. Examine the convergence of the solution for the given problems.
5. Compare various methods and choose the best method to solve the problems.

## UNIT I

## 18 hours

Iteration method based on Second degree equations - Chebyshev Method Multipoint Iteration Methods - Bridge Vieta Method - Baristow Method - Graeffe's root Squaring Method.

UNIT II
18 hours
Iteration Methods - Jacobi Method - Guass Seidel Method - Successive Over Relaxation Method - Iterative Method for A $^{-1}$ - \#Eigen Values and Eigen Vectors\# - Jacobi Method for symmetric Matrices - Power Method.

## UNIT III

## 18 hours

Interpolation and Approximation - Hermite Interpolation - Piecewise cubic Interpolation and cubic Spline interpolation - Bivariate interpolation - Lagrange and Newton's Bivariate interpolation - \#Least Square approximation\# - Gram-Schmidt Orthogonalizing Process.

UNIT IV

## 18 hours

Differentiation and Integration: Numerical Differentiation - Methods Based on Interpolation -Partial Differentiation - Numerical Integration - Methods Based on Interpolation - Methods Based on Undetermined Coefficients - Gauss Quadrature methods - Gauss Legendre and Gauss ChebyshevIntegration Methods - Double Integration Trapezoidal and Simpson's Rule - Simple Problems.

UNIT V
Ordinary Differential Equations: Numerical Methods - Euler Method - \#Backward Euler Method\# - Mid-Point Method - Runge-kutta Methods - Implicit Runge-Kutta Methods - Predictor - Corrector Methods.

## \# \# Self-study portion.

## Text Book:

M.K. Jain, S.R.K. Iyengar, R.K. Jain, Numerical Methods for Scientific and Engineering Computation, New Age International Private Ltd, Sixth Edition (2012).

| UNIT I | Chapter II | Sections 2.4, 2.9 |
| :--- | :--- | :--- |
| UNIT II | Chapter III | Sections 3.4, 3.5,3.7, 3.11 |
| UNIT III | Chapter IV | Sections 4.5, 4.6, 4.7, 4.9 |
| UNIT IV | Chapter V | Sections 5.2, 5.5, 5.6, 5.7, 5.8, 5.11 |
| UNIT V | Chapter VI | Sections 6.3, 6.4, 6.7 |

## Books for Reference:

1. Samuel. D. Conte and Carl De Boor, Elementary Numerical Analysis, McGraw Hill Company, Third Edition (1965).
2. F.B. Hildebrand, Introduction to Numerical Analysis, Tata McGraw Hill Company,2 ${ }^{\text {nd }}$ Edition (1974).

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| II | 20PMA2CC8 |  |  | NUMERICAL ANALYSIS |  |  |  | 6 | 4 |  |
| Course Outcomes (COs) | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  |
| CO2 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO3 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO4 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| CO5 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| Number of Matches= 39, Relationship : HIGH |  |  |  |  |  |  |  |  |  |  |

## Prepared By:

Dr.A. Mohamed Ismayil
Ms. HyroonBee

Checked by:
Dr.U.Abuthahir

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| II | 20PMA2DE2A | DSE - II | FUZZY <br> ANALYSIS AND <br> ITS | 6 | 4 | 100 | 25 | 75 |

## Course Outcome:

At the end of the Course, Students will be able to:
1: Apply domain knowledgefrom classical sets to fuzzy sets with illustrations.
2: Describe the fuzzy arithmetic, Linguistic variables and examine Fuzzy equations.
3: Determine fuzzy logic and fuzzy propositions.
4: Examine fuzzy Decision making problem and Fuzzy Linear programming problem.
5: Classify fuzzy relations and properties of fuzzy relations.

## UNIT I

18 hours
From Classical Sets to Fuzzy sets - Fuzzy set: Basic types - Fuzzy sets Versus Crisp setsExtension Principle for fuzzy sets - Operations on Fuzzy sets - \#Types of operations\# - Fuzzy complements.

## UNIT II

## 18 hours

Fuzzy Arithmetic - Fuzzy numbers - Linguistic variables - Arithmetic operations on intervals -Arithmetic operations on Fuzzy numbers -Lattice of Fuzzy numbers- Fuzzy equations.

## UNIT III

## 18 hours

Fuzzy Logic - Multi-valued Logics - Fuzzy Propositions - Unconditional and Unqualified Fuzzy propositions - Unconditional and qualified Propositions - Conditional and Unqualified propositions -Conditional and Qualified propositions - Linguistic Hedges - Inference from conditional Fuzzy propositions- \#Inference from conditional and qualified propositions\#.

## UNIT IV

## 18 hours

Fuzzy Decision making - \#Individual decision making\# - Fuzzy Ranking methods - Fuzzy Linear programming.

## UNIT V

18 hours
Fuzzy Relations - Composition of fuzzy relations - Properties of fuzzy relations.

## \# \#-Self study

## Text Books:

T.B-1 George J. Klir and Bo Yuan, Fuzzy sets and Fuzzy Logic Theory and Applications, Prentice Hall of India, (2004).
T.B-2 A. Nagoor Gani and V.T. Chandrasekaran, A first look at Fuzzy Graph Theory, Allied Publishers Pvt. Ltd., (2010).

| UNIT I | Chapter 1 | Sections 1.3, 2.3 |  |
| :--- | :--- | :--- | :--- |
|  | Chapter 3 | Sections 3.1\&3.2 | T.B-1 |
| UNIT II | Chapter 4 | Sections 4.1-4.6 | T.B-1 |
| UNIT III | Chapter 8 | Sections 8.2, 8.3, 8.5-8.7 | T.B-1 |
| UNIT IV | Chapter 15 | Sections 15.2, 15.6, 15.7 | T.B-1 |
| UNIT V | Chapter 1 | Sections 1.3-1.5 | T.B-2 |

## Books for Reference:

1. H.J. Zimmermann, Fuzzy Set Theory and its Applications, Allied Publishers Limited (1991).
2. M. Ganesh, Introduction to Fuzzy sets and Fuzzy logic, Prentice Hall of India, New Delhi (2006).

## Web Source:

https://nptel.ac.in/courses/108/104/108104157/ https://nptel.ac.in/courses/111/102/111102130/ https://nptel.ac.in/courses/127/105/127105006/

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours | Credits |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| II | 20PMA2DE2A |  |  | FUZZY ANALYSIS AND ITS APPLICATIONS |  |  |  | 6 | 4 |  |
| Course Outcomes (COs) | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO2 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| CO3 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO4 |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO5 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| Number of Matches= 39, Relationship : HIGH |  |  |  |  |  |  |  |  |  |  |

## Prepared by :

Dr. A. Nagoor Gani
Dr. H. Sheik Mujibur Rahman

Checked by :
Dr.M.Mohamed Althaf

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| II | 20PMA2DE2B | DSE - II | MATHEMATICAL <br> METHODS IN <br> BIOLOGY | 6 | 4 | 100 | 25 | 75 |

## Course Outcome:

At the end of the Course, Students will be able to:

1. Discuss the sequence alignments, alignment graphs and CDNA matching with illustrations .
2. Demonstrate the Multiple sequence alignments and Multifunction tools for sequence analysis .
3. Explain the Phylogenetic analysis, Evolutionary Trees and Phylogeny with examples.
4. Apply the domain knowledge for SQL,DDL, DML and TLC commands.
5. Determine the bioinformatics tools for database search using engines.

## UNIT I

18 hours
Sequence alignments, Basic string definitions, The importance of sequence comparison in Molecular Biology, The edit distance between two strings, String alignment, Edit graphs, String similarity, Alignment graphs, Local alignment, Introduction to Gaps, CDNA matching, A concrete illustration, Choices for gap weights, Time analysis.

## UNIT II

18 hours
Overview of RDBMS, Advantages of DBNS, Normalization, Oracle data types, Introduction to SQL, DDL, DML, \& TLC commands. Data definition Language, Data Manipulation Language, Transaction Control \& data, Control language Grant \& Revoke Privilege Command.

UNIT III
18 hours
Multiple sequence alignments, the morphological to the molecular, Common multiple alignment methods, multiple sequence alignments, Local alignment gaps, parametric sequencealignments, suboptimal alignments, Multifunction tools for sequence analysis.

## UNIT IV

18 hours
Phylogenetic analysis, Evolutionary Trees and Phylogeny, Ultrasonic trees, Parsimony, Ultrametric problem, Perfect phylogeny, Phylogenetic alignment, Connection between multiplealignment and tree construction, Methods in Phylogeneic Analysis, Profiles and Motifs

## UNIT V

18 hours
Tools in Bioinformatics, Tools for database search using search engines, Finding scientific articles, Finding public data bases, Depositing data into public data bases, Tools for Sequence Analysis, Algorithms issues in data base search, FASTA, BLAST, Amino acid substitution matrices PAM and BLOSSUM

## Text Books:

1. George Koch and Kevin Loney; ORACLE 8-THE COMPLETE REFERENCE, Tata McGraw - Hill Edition, 1988.
2. Michael Abbey andMichael J. Correy; ORACLE 8 - A BEGINNERS GUIDE, 1997.
3. Eddy, S.R., Durbin et al; Computational Molecular Biology, 2002.
4. Cynthia Gibas\& Per Jampeck, Developing Bioinformatics ComputerSkills; Shroff Publishers and Distributors Private Limited, Calcutta, 2001.
5. Waterman,Michael S, Introduction to Computational Biology, Chapman and Hall, CRC Press, 2000.

## Books for Reference:

1. Baxevanis, A.D., and Ouellette, Francis, B.F., Bioinformatics - A practical Guide to theAnalysis
of genes and Proteins, JohnWiley and Sons Inc. Publishing, New York, 1998.
2. Dan Gusfield, Algorithms on Strings, trees and sequences, Cambridge University Press, USA.

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific
Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 20PMA2DE2B |  |  | MATHEMATICAL METHODS IN BIOLOGY |  |  |  | 6 | 4 |  |
| Course Outcomes (COs) | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO2 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  |
| CO3 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO4 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| CO5 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| Number of Matches= 36, Relationship : HIGH |  |  |  |  |  |  |  |  |  |  |

Prepared by :
Dr.A.Nagoor Gani

Checked by :
Dr.M.Mohamed Althaf

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| III | 20PMA3CC9 | Core - IX | FUNCTIONAL <br> ANALYSIS | 6 | 5 | 100 | 25 | 75 |

## Course Outcomes

1. To acquire more knowledge on Banach space through Hahn Banach theorem
2. Demonstrate and discuss Open mapping theorem and Conjugate of an operator.
3. Apply domain knowledge for Hilbert Space.
4. Remember the theorem based on the Hilbert space with an operator.
5. Classification and study of finite dimensional spectral theory.

## UNIT I

18 hours
Banach Space: Definition and some examples - Continuous linear transformations -Hahn Banach theorem.

## UNIT II

18 hours
Banach space (continued): Natural imbedding of $N$ in $N^{* *}$ - The open mapping theorem -The conjugate of an operator.

## UNIT III

18 hours
Hilbert spaces: Definition and some simple properties - Orthogonal complements -Orthonormal sets - The conjugate space $\mathrm{H}^{*}$.

## UNIT IV

18 hours
Hilbert spaces (Continued): The adjoint of an operator - Self-adjoint operators - Normal andunitary operators \#Projections\#.

## UNIT V

## 18 hours

Finite-Dimensional spectral theory: Matrices - Determinants and the spectrum of anoperator - The spectral theorem.

## \# \# Self-study portion.

## Text Books:

G.F Simmons, Introduction to Topology and Modern Analysis, McGraw Hill, International Book Company, 2014. (21st reprint).

| UNIT I | Sections | $46-48$ |
| :--- | :--- | :--- |
| UNIT II | Sections | $49-51$ |
| UNIT III | Sections | $52-55$ |
| UNIT IV | Sections | $56-59$ |
| UNIT V | Sections | $60-62$ |

## Books for Reference:

1. Balmohan V. Limaye, Functional Analysis, New Age International Pvt. Ltd., Second Edition (2005).
2. M. Thamban Nair, Functional Analysis, A First Course, Prentice Hall of India (2002).
3. Sudhir Kumar Pundir, Functional Analysis, CBS Publishers and Distributors Pvt. Ltd., (2016).

## Web Source

1. https://youtu.be/M1h915p95Yk
2. https://youtu.be/5BfJHZRgoEA
3. https://youtu.be/xaHkXIWcgP8
4. https://youtu.be/96HNI6M4mCl
5. https://youtu.be/i7LABYdOm4o
6. https://youtu.be/s-5bCfENHg8
7. https://youtu.be/8DtYIUgike8
8. https://youtu.be/mVGhIWf-CEU

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:


## Prepared by:

1.Dr. A. Mohamed Ismayil

Checked by:

1. Dr. U. Abuthahir

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| III | 20PMA3CC10 | Core $-X$ | PARTIAL DIFFERENTIAL <br> EQUATIONS | 6 | 5 | 100 | 25 | 75 |

## Course Outcomes

1. Recognize and recall the basic concept of first order P.D.E and classification of integrals with examples.
2. Show and illustrate the examples of Jacobi's method and quasi-linear equations
3. Demonstrate the examples for one dimensional wave equations and vibrations of a string
4. Discuss the boundary value problems in second order PDE's
5. Classify heat conduction and wave equation with examples.

## UNIT I

18 hours
Curves and Surfaces-Genesis of First Order P.D.E-Classification of Integrals-Linear equations of the First OrderPfaffian Differential Equations-Compatible Systems-Charpit's method.

## UNIT II

## 18 hours

Jacobi's Method-Integral Surfaces Through a given Curve-Quasi-Linear Equations.
UNIT III

## 18 hours

Genesis of Second Order P.D.E-Classification of Second order P.D.E-One Dimensional Wave Equations-Vibrations of an Infinite String-Vibrations of a Semi-infinite string-\#Vibrations of a string of Finite length\#.

## UNIT IV

18 hours
Vibrations of a String of Finite length (Method of Separations of Variables)-Laplace Equation-Boundary Value Problems-Maximum and Minimum Principles-The Cauchy Problem The Dirichlet Problem for the Upper Half Plane- The Neumann Problem for the Upper Half Plane-The Dirichlet Problem for a circle-The Dirichlet Exterior Problem for a circle-\#The Dirichlet Problem for a Rectangle\#.

## UNIT V

## 18 hours

The Dirichlet Problem for a Half Plane-The Dirichlet Problem for a circle-Heat Conduction Problem-Heat ConductionInfinite rod case-Heat Conduction-Finite Rod case Duhamel's Principle-Wave Equation-\#Heat Conduction Equation\#.

## \# \# Self-study portion.

## Text Books:

T.Amarnath, An Elementary Course in Partial Differential Equations, Second Edition, Narosa Publishing House-2003.

| UNIT I | Chapter I | Sections 1.1-1.7 |
| :--- | :--- | :--- |
| UNIT II | Chapter I | Sections 1.8-1.10 |
| UNIT III | Chapter II | Sections 2.1-2.3.3 |
| UNIT IV | Chapter II | Sections 2.3.5-2.4.9 |
| UNIT V | Chapter II | Sections 2.4.12-2.6.2 |

## Books for Reference:

1. I.N.Sneddon, Elements of partial differential Equations, McGraw Hill,1985.
2. M.D.Raisinghania, Advanced differential equations, Seventh revised edition S.Chand and Company Ltd, New Delhi, 2000.

## Web Source

1. https://nptel.ac.in/courses/111/103/111103021/
2. https://youtu.be/YLsNeg00p5M
3. https://youtu.be/FZZS91nfRgc
4. https://youtu.be/I3T4SL6IEIE
5. https://youtu.be/cNLMDPfWJeA
6. https://youtu.be/DDPO-19FyJM
7. https://youtu.be/S6w0sumMyAs
8. https://youtu.be/HFPLdAKCVRU
9. https://youtu.be/aolvx8bWFDA

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| III | 20PMA3CC10 |  |  | PARTIAL DIFFERENTIAL EQUATIONS |  |  |  | 6 |  | 5 |
| Course Outcomes | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 |
| CO1 |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  |  |
| CO 2 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO3 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO4 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| CO5 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| Number of Matches= 36, Relationship : High |  |  |  |  |  |  |  |  |  |  |

## Prepared by:

1.Dr. A. Prasanna
2. Ms. A. Nafiunisha

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| III | 20PMA3C11 | Core - XI | MODERN <br> PROBABILITY <br> THEORY | 6 | 4 | 100 | 25 | 75 |

## Course Outcomes

1. Recall and discuss the Booles inequality and discrete probability space with examples.
2. Examine Study Jordan decomposition theorem and inequalities with examples.
3. Investigate the convergence of random variables and convergence in distribution.
4. Determine the laws of large numbers and SLLN for i.i.d case with illustrate the examples.
5. Prove central limit theorem and Lindeberg-Feller theorem.

## UNIT I

18 hours
Probability: Definition of Probability-Axiomatic-Definition-Some Properties-Booles inequality- Discrete Probability Space-General Probability Space-Induced Probability Space-Conditional Probability Measure.

## UNIT II

## 18 hours

Distribution function of a Random Variable-Decomposition of D.F's-Jordan Decomposition Theorem-Distribution functions of Vector Random Variables-Bivariate case only- Correspondence Theorem. Expectation and Moments: Definition of Expectation -properties of Expectation -Definition of Moments-Moment Generating Function- $\mathrm{C}_{\mathrm{r}}$ -inequality-Holder's inequality-Schwarz's inequality-Minkowski inequality.

## UNIT III

## 18 hours

Convergence of Random Variables: Convergence in Probability-Convergence almost surely-Convergence in Distribution-Convergence in $\mathrm{r}^{\text {th }}$ Mean-Monotone Convergence Theorem-Fatou's Theorem-Dominated Convergence Theorem.

## UNIT IV

## 18 hours

Laws of Large Numbers: Convergence of a Series of Independent Random Variables-Kolmogorov inequalities and almost surely Convergence- Kolmogorov three-Series Theorem -Stability of Independent Random Variables-Weak Law of Large numbers-Kronecker's Lemma-WLLN-IID Case- Khintchine's WLLN-Strong Law of Large Numbers-KolmogorovSLLN for i.i.d case.

## UNIT V

18 hours
Central Limit Theorem: Introduction -Lindeberg-Levy Theorem-Variable Distributions: Liapounov’s Theorem-Lindeberg-Feller Theorem.

## \# \# Self-study portion.

## Text Books

B.R.Bhat, Modern Probability Theory, Fourth Edition, New Age International, 2014.

| UNIT I | Chapter 3 | Sections 3.1-3.6 |
| :--- | :--- | :--- |
| UNIT II | Chapter 4 | Sections 4.1-4.4 |
|  | Chapter 5 | Sections 5.1-5.3 |
| UNIT III | Chapter 6 | Sections 6.1-6.5 |
| UNIT IV | Chapter 10 | Sections 10.1-10.3 |
| UNIT V | Chapter 11 | Sections 11.1-11.3 |

## Books for Reference:

1. Fisz, Probabaility theory and Mathematical Statistics, Third Edition, John Willey \&Sons 1963.
2.Murry R.Spiegal,John Jschiller,R.Aly Srinivasan,Probability and Statitcs,Third Edition,Shaum’s Outline Series,2010.

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:


## Prepared by:

1.Dr.P.Muruganantham

## Checked by:

1. Ms.A.Thagasin Banu

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| III | 20PMA3CC12 | Core - XII | ADVANCED <br> GRAPH THEORY | 6 | 4 | 100 | 25 | 75 |

## Course Outcomes

1. Apply domain knowledge connectivity and edge-connectivity withillustrations.
2. Demonstrate and discuss matching and stable matching.
3. Bring out Independent sets and prove Vizing's Theorem.
4. Determine the predecessor and successor algorithm.
5. Discuss the concepts of perfect graphs and interval graphs.

## UNIT I

## 18 hours

Connectivity and edge-connectivity - 2-connected graphs - Menger's theorem.

## UNIT II

18 hours
Matching - System of Distinct Representatives and Marriage problem - Covering - 1-factor - Stable Matching.

## UNIT III

18 hours
Independent sets - Edge-colourings - Vizing's Theorem - Vertex Colourings - Uniquely Colourable graphs - Critical graphs.

## UNIT IV

18 hours
Predecessor and Successor - Algorithm - Graceful Labeling - Sequential functions - Magic graphs - Conservative graphs.

## UNIT V

## 18 hours

Perfect Graphs - Perfect Graph Theorem - Chordal Graphs - Interval Graphs - Comparability Graphs.

## \# \# Self-study portion.

## Text Books:

M. Murugan, Topics in Graph theory and Algorithms, Muthali Publishing House, Annanagar, Chennai, First Edition (2003).

| UNIT I | Chapter 3 | Sections 3.1-3.3 |
| :--- | :--- | :--- |
| UNIT II | Chapter 6 | Sections 6.1-6.5 |
| UNIT III | Chapter 7 | Sections 7.1, 7.2, 7.4-7.7 |
| UNIT IV | Chapter 10 | Sections 10.1-10.4, 10.6, 10.7 |
| UNIT V | Chapter 12 | Sections 12.1-12.5 |

## Books for Reference:

1. S. Arumugam and S. Ramachandran, Invitation to Graph Theory, New Gamma Publishing House, Palayamkottai, 2006.
2. S.A. Choudum, First Course in Graph Theory, Macmillan India Limited, New Delhi (2009).
3. F. Harary, Graph Theory, Addison-Wesley Publishing Company, INC. (1969).

## Web Source

1. https://www.youtube.com/watch?v=mNzg7CoF3r0\#action=share
2. https://www.youtube.com/watch?v=7UZGUiG-UCw\#action=share
3. https://www.youtube.com/watch?v=Ea3DICocONQ\#action=share

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| III | 20PMA3CC12 |  |  | ADVANCED GRAPH THEORY |  |  |  | 6 | 4 |  |
| Course Outcomes (COs) | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 |  | PSO3 | PSO4 | PSO5 |
| CO1 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO2 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| CO3 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  |  | $\checkmark$ | $\checkmark$ |  |
| CO4 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO5 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| Number of Matches= 38, Relationship : High |  |  |  |  |  |  |  |  |  |  |

Prepared by:
1.Dr. R. Jahir Hussain

## Checked by:

1. Dr. H. Sheik Mujibur Rahman

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| III | 20PMA3DE3AT | DSE - III | PYTHON <br> PROGRAMMING | 3 | 2 | 50 | 10 | 40 |

## Course Outcomes

1. To provide introduction to comments, operators, variables andPython Objects.
2. Explain Standard Type operators, numbers and built-in Functions in python programming.
3. Learn strings, lists and tuples in Python programming.
4. Implement conditionals and loops for Python Programs.
5. To construct regular expressions and network programming in Python.

## UNIT I

15 Hours
What is Python - Origins of Python - Features of Python -Downloading and Installing Python - Running Python Comments - Operators - Variables and Assignment - Python Objects - Standard Types - Other Built-in Types.

## UNIT II

## 15Hours

Internal Types - Standard Type Operators - Standard Type Built-in Functions - Categorizing the Standard Types Unsupported Types - Introduction to Numbers - Integers - Floating Point Real Numbers - Complex Numbers - Operators - Built-in Functions -Sequences.

## UNIT III

## 15Hours

Strings - Strings and Operators - String-only Operators - Built-in Functions - String Built-in Methods - Special Features of Strings - Lists - Operators - Built-in Functions - List Type Built-in Methods - Special Features of Lists - Tuples - Tuple Operators and Built-in Functions - Special Features of Tuples .

## UNIT IV 15Hours

Conditionals and Loops - if statement - else statement - else if statement - while statement - for statement - break statement - continue statement - pass statement - else statement -File Objects - File Built-in Function - File Built-in Methods - File Built-in Attributes - Standard Files -Command-line Arguments - File System - File Execution - Persistent Storage Modules

## UNIT V

## 15Hours

Regular Expressions - Introduction - Special symbols and characters for Regular Expressions - Regular Expressions and Python - Network Programming - Introduction - Network programming in Python - Sockets : Communication end points.
\# \# Self-study portion.

## Text Books:

Chun, J Wesley, CORE Python Programming, 2nd Edition, Pearson, 2007 Reprint 2010.

| UNIT I | Chapter 1 | Section -1.1 to 1.5 <br>  <br>  <br>  <br> Chapter 2 |
| :--- | :---: | :---: |
| Chapter 4 | Section- 2.3 to 2.5 |  |
| UNIT II | Chapter 4 | Section-4.1 to 4.3 |
|  | Chapter 5 | Section $-4.4,4.5,4.6,4.8,4.9$ |
| UNIT III | Chapter 6 | Section- 5.1 to 5.6 |
| UNIT IV | Chapter 8 | Section-6.2 to 6.7 to 8.10 |
|  | Chapter9 6.11 to 6.18 |  |
| UNIT V | Chapter 15 | Section -9.1 to 9.9 |
|  | Chapter 16 | Section-15.2,15.3 |
|  |  | Section- 16.1,16.2,16.3 |

## Books for Reference:

1. Jeffrey Elkner, Chris Meyers Allen Downey, Learning with Python, Dreamtech Press, 2015.

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| III | 20PMA3DE3AT |  |  | PYTHON PROGRAMMING |  |  |  | 3 | 2 |  |
| Course Outcomes | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 |  | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO2 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ |  |
| CO3 |  |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO4 | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  |
| CO5 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| Number of Matches= 32, Relationship : Moderate |  |  |  |  |  |  |  |  |  |  |

Prepared by:
1.Dr. M. Mohamed Jabarulla

## Checked by:

1. Dr. S. Shajitha Begum

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| III | 20PMA3DE3AP | DSE - III | PYTHON <br> PROGRAMMING <br> - Practical | 3 | 2 | 50 | 10 | 40 |

## Objective:

To enable the students acquire programming skills by applying various features of Python Language.

## List of Practical:

1. Program to demonstrate arithmetic operations.
2. Program using numbers and operators.
3. Program using string built-in functions.
4. Program using functions and modules.
5. Program using lists.
6. Program using tuples.
7. Program using conditional statement.
8. Program using looping statement.
9. Program using continue, pass and else statement.
10. Program to read and write file.

Prepared by:

## Checked by:

1.Dr. M. Mohamed Jabarulla

1. Dr. S. Shajitha Begum

| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| III | 20PMA3DE3B | DSE - III | COMPUTER | ALGORITHMS | 6 | 4 | 100 | 25 |

## UNIT I

18 hours
Algorithm - Definition, Time Complexity. Elementary Data Structures - Stacks, Queues, Trees, Priority Queues, Heaps, Heapsort, Graphs.

## UNIT II

18 hours
Divide and Conquer - General method, Binary search, Merge sort, Quick sort.

## UNIT III

18 hours
The Greedy Method - Knapsack problem, Job sequencing with dead lines, Optimal storage on tapes, Optimal merge patterns.

## UNIT IV

18 hours
Basic traversal - Inorder, preorder, postorder traversals, Breadth first search and traversal, Depth first search and traversal Backtracking - Sum of subsets, $n$-Queens problem ( $n=4,8$ ).

## UNIT V

## 18 hours

NP - Hard and NP - complete problems - Basic Concepts, Cook's Theorem(Statement only), Conjunctive Normal Form(CNF) - satisfiability reduces to Clique Decision Problem(CDP), The Clique Decision Problem(CDP) reduces to The Node Cover Decision Problem .

## \# \# Self-study portion.

## Text Book:

Ellis Horowitz, SartajSahni, Sanguthevar Rajasekaran, 'Fundamentals of Computer Algorithms', Galgotia Publications, 1998.

| UNIT I | Chapter I | Section 1.1 |
| :--- | :--- | :--- |
|  | Chapter II | Sections 2.1-2.5 |
| UNIT II | Chapter III | Sections 3.1-3.5 |
| UNIT III | Chapter IV | Sections 4.1-4.5 |
| UNIT IV | Chapter VI | Section 6.1 |
|  | Chapter VII | Sections 7.1-7.3 |
| UNIT V | Chapter XI | Sections 11.1-11.3 |

## Books for Reference:

1. Thomas H.Cormen, Charles E. Leiserson, Ronald L. Rivest, Clifford Stein, 'Introduction toAlgorithms', Second Edition, Prentice Hall of India, 2004.
2. Alfred V.Aho, John E.Hopcroft and Jeffrey D.Ullman, 'Data Structures and Algorithms',Addison-Wesley, 1983.
3. M. Gary and S. Johnson, 'Computers and Interactability: A guide to theory of NPCompleteness',W. H. Freeman \& Company, 1979.

| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| IV | 20PMA4CC13 | Core - XIII | MEASURE <br> THEORY AND <br> INTEGRATION | 6 | 5 | 100 | 25 | 75 |

## Course Outcomes

1. Apply domain knowledge for Measure on a real line and illustrate with examples.
2. Discuss the concepts of Borel and Lebesgue measurability with suitable examples
3. Explain the abstract measure space with the examples.
4. Determine the Almost uniform convergence and study decomposition of measure.
5. Prove the Radon Nikodym theorem and Fubini's theorem.

## Unit I

## 18hours

\#Set function and properties on sets in real line\# -Measure on a real line - LebesgueOuter measure - Measurable sets Regularity - Measurable functions.

## Unit II

18 hours
\#Borel set- Continuous function and integral function\# - Borel and Lebesgue measurability - Integration of Functions of a real variable - Integration of non-negative functions - General Integral.

## Unit III

18 hours
\#Measure on measurable space\# - Abstract Measure Space - Measure and Outer measure - Uniqueness of the extension - Completion of a measure - Measure space - Integration with respect to measure.

## Unit IV

18 hours
\#Countable and additive\# - Convergence in measure - Almost uniform convergence - Signed measure and their derivatives - Hahn Decomposition - Jordan Decomposition.

## Unit V

18 hours
\#Product space\# - RadonNikodym theorem - Measure and Integration in a Product space - Measurability in a Product Space - Product Measure and Fubini's theorem.

## \# \# Self-study portion.

## Text Books:

G. De Barra,Measure Theory and Integration, New Age International (P) Limited, Publishers, New Delhi Fourth Reprint, (1997).

| UNIT I | Sections 2.1-2.4 |
| :--- | :--- |
| UNIT II | Sections $2.5,3.1-3.2$ |
| UNIT III | Sections 5.1-5.6 |
| UNIT IV | Sections 7.1,7.2,8.1,8.2 |
| UNIT V | Sections 8.3, 10.1, 10.2 |

## Books for Reference:

1. M. C. Munroe, Measure and Integration, Addison, Wesley Publishing Company, Second Edition (1971).
2. H.L. Roydon and P.M. Fitzpatrick, Real Analysis, Prentice Hall of India, Learning Pvt. Ltd., New Delhi, Four Edition (2011).

## Web Source

1. https://youtu.be/Uh 91ffyWr4
2. https://youtu.be/wmL29BLgrW4
3. https://youtu.be/3sBfw IEEX4
4. https://youtu.be/JBRuOyAbOqM
5. https://youtu.be/ wThvhkiH5M

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours |  | Credits |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| IV | 20PMA4CC13 |  |  | MEASURE THEORY AND INTEGRATION |  |  |  | 6 | 5 |  |
| Course Outcomes | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
| (COs) | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 |  | PSO3 | PSO4 | PSO5 |
| CO1 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO2 |  |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| CO3 | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ |
| CO4 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  |
| CO5 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| Number of Matches= 36, Relationship : High |  |  |  |  |  |  |  |  |  |  |

## Prepared by:

1.Ms. M. S. Afya Farhana

Checked by:

1. Dr. D. Dhamodharan

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| IV | 20PMA4CC14 | Core - XIV | FLUID <br> DYNAMICS | 6 | 5 | 100 | 25 | 75 |

## Course Outcomes

1. Demonstrate and discuss fluid flows, stream lines, vorticity vector and equation of continuity with examples.
2. Derive the Euler's equation of motion and Bernoulli's equation with the examples.
3. Distinguish sources, sinks and doublets and analyze the axis-symmetric flows and stokes stream function.
4. Determine the concept of two-dimensional flows and complex potential flows.
5. Acquire the Milne-Thomson circle theorem and theorem of Blasius and illustrate some applications of the circle theorem.

## UNIT I

18 hours
Real fluids and ideal fluids - Velocity of a fluid at a point - Streamlines and pathlines - Steady and unsteady flows. Velocity potential - Vorticity vector - \#Local and particle rates of change\# - Equation of continuity - Worked examples \#Acceleration of a point of a fluid\#.

## UNIT II

## 18 hours

Pressure at a point in a fluid at rest - Pressure at a point in a moving fluid - \#Conditions at a boundary of two inviscid Immissible fluids\# - Euler's equations of motion - Bernoulli's equation - Worked examples - Some flows involving axial symmetry - Some special two dimensional flows - \#Impulsive motion\#.

## UNIT III

## 18 hours

Some three dimensional flows - Sources, sinks and doublets - \#lmages in a rigid infinite plane\# - Axis-symmetric flows - Stokes stream function - Some special forms of the stream function for Axis-symmetric irrotational motions.

## UNIT IV

18 hours
Two dimensional flow - Use of cylindrical polar coordinates - Stream function. \#Complex potential for twodimensional irrotational - Incompressible flow\# - Complex velocity potential for standard two-dimensional flows Uniform stream, line sources and line sinks, line doublets, line vortices - Worked examples.

## UNIT V

## 18 hours

Two dimensional image systems - Milne-Thomson circle theorem - Some applications of the circle theorem - Extension of the circle theorem - Theorem of Blasius - \#Use of conformal transformation - Some hydro dynamical aspects of conformal transformation\# - Worked example.

## \# \# Self-study portion.

## Text Books:

F. Chorlton, Textbook of Fluid Dynamics, CBS Publication and Distribution (2004).

| UNIT I | Chapter 2 | Sections 2.1 to 2.9 |
| :--- | :--- | :--- |
| UNIT II | Chapter 3 | Sections 3.1 to 3.6, 3.9 to 3.11 |
| UNIT III | Chapter 4 | Sections 4.1 to 4.3, 4.5, 4.5.1 |
| UNIT IV | Chapter 5 | Sections 5.1 to 5.6 |
| UNIT V | Chapter 5 | Sections 5.7 to 5.10.2 |

Books for Reference:
1.Goyal and Gupta, Fluid Dynamics,Edition 17, PragatiPrakashan ,(2011).
2. Raja Subramanian,Fluid Mechanics -Introduction and Application, Jaicopublishing houseEdition 2(2008).

## Web Source

1. https://nptel.ac.in/courses/103/106/103106159/
2. https://nptel.ac.in/courses/112/105/112105269/
3. https://www.youtube.com/watch?v=TaUXPnIFd6Q
4. https://www.youtube.com/watch?v=luGzHVdE4TE
5. https://www.youtube.com/watch?v=3AcTSjvTnnA
6. https://www.youtube.com/watch?v=etjEykTm95s
7. https://www.youtube.com/watch?v=vcNvhnqC68A
8. https://www.youtube.com/watch?v=UM-pkVPw4tE

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours | Credits |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| IV | 20PMA4C14 |  |  | FLUID DYNAMICS |  |  |  | 6 | 5 |  |
| Course Outcomes | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 | PSO2 | PSO3 | PSO4 | PSO5 |
| CO1 |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| CO 2 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| CO3 |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO4 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  |  |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO5 | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| Number of Matches= 36, Relationship : High |  |  |  |  |  |  |  |  |  |  |

Prepared by:
1.Dr. S. Mohamed Yusuff Ansari

Checked by:

1. Ms.S.Sharmila Banu

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| IV | 20PMA4CC15 | Core - XV | INTEGRAL EQUATIONS <br> AND CALCULUS OF <br> VARIATIONS | 6 | 5 | 100 | 25 | 75 |

## Course Outcomes

1. Discuss the basic concepts of eigen values and eigen functions with illustrate the examples.
2. Determine the method of successive approximations and Volterra integral equations with suitable examples.
3. Study of applications to ordinary differential equations and solve the Abel integral equations.
4. Applying domain knowledge for maxima and minima illustrate the examples.
5. Bring out natural boundary conditions and transition conditions withlllustrations.

## UNIT I

18 hours
Regularity conditions - Special kinds of kernels - Eigen values and Eigen functions - Convolution Integral - Inner or Scalar product of two functions. Integral equations with separable kernels - Reduction to a system of Algebraic Equations - \#Examples\# - Fredholm Alternative - \#Examples\#.

## UNIT II

## 18 hours

Method of successive approximations - Iterative scheme - \#Examples\# - Volterra IntegralEquations - \#Examples\# - Some results about the resolvent Kernel.

## UNIT III

## 18 hours

Applications to ordinary differential equations - Initial value problems - Boundary valueProblems - \#Examples\# Singular integral equations - Abel Integral Equation - \#Examples\#.

## UNIT IV

18 hours
Calculus of variations and applications - Maxima and Minima - Simplest case - \#lllustrativeexamples\#.

## UNIT V

18 hours
Natural Boundary conditions and transition conditions - Variational notation - \#More general case \# - Constraints and Lagrange multipliers.

## \# \# Self-study portion.

## Text Books:

T.B-1 Ram P. Kanwal, Linear Integral Equations Theory and Technique, Academic Press, Birkhäuser, New York (2013).
T.B-2 Francis B. Hildebrand, Methods of Applied Mathematics, Dover, Prentice Hall of India, New York, Dover, Second Edition (1992).

| UNIT I | Sections $1.1-1.6,2.1-2.4$ | T.B-1 |
| :--- | :--- | :--- |
| UNIT II | Sections $3.1-3.5$ | T.B-1 |
| UNIT III | Sections $5.1,5.2,5.3,8.1,8.2$ | T.B-1 |
| UNIT IV | Sections $2.1,2.2,2.3$ | T.B-2 |
| UNIT V | Sections $2.4-2.7$ | T.B-2 |

## Books for Reference:

1. Sudir K. Pundir and Rimple Pundir, Integral Equations and Boundary Value Problems, Pragati Prakasam, Meerut (2005).
2. M. D. Raisinghania, Integral Equations and Boundary Value Problems, S. Chand \& Co., New Delhi (2007).

## Web Source

1. https://nptel.ac.in/courses/111/107/111107103/
2. https://youtu.be/WPIBrzj|1KI?t=804
3. https://youtu.be/K0t53t7RLWY?t=132
4. https://youtu.be/rCWzF1yvZIQ
5. https://youtu.be/u4yhu8QMC2M
6. https://youtu.be/76P7MS-Y1Bk
7. https://youtu.be/Ccng6vYW-i0?t=190
8. https://youtu.be/BVf9tkJaiu0?t=454
9. https://youtu.be/eL4cgrLIkUo
10. https://youtu.be/SLzFIZUJkzO

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:

| Semester | Code |  |  | Title of the Paper |  |  |  | Hours | Credits |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| IV | 20PMA4CC15 |  |  | INTEGRAL EQUATIONS AND CALCULUS OF VARIATIONS |  |  |  | 6 | 5 |  |
| Course Outcomes | Programme Outcomes (POs) |  |  |  |  | Programme Specific Outcomes (PSOs) |  |  |  |  |
| (COs) | PO1 | PO2 | PO3 | PO4 | PO5 | PSO1 |  | PSO3 | PSO4 | PSO5 |
| CO1 |  |  | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| CO2 | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ |
| CO3 |  | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| CO4 | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| CO5 | $\checkmark$ | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  | $\checkmark$ |
| Number of Matches= 36, Relationship : High |  |  |  |  |  |  |  |  |  |  |

Prepared by:
1.Dr. M. Mohamed Jabarulla

## Checked by:

1. Dr. D. Dhamodharan

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| IV | 20PMA4DE4A | DSE - IV | ADVANCED <br> OPERATIONS <br> RESEARCH | 6 | 4 | 100 | 25 | 75 |

## Course Outcomes

1. Discuss the basic concepts of integer linear programming and sensitivity analysiswith examples.
2. Construct the goal programming problem and general goal programming model.
3. Investigate the decision making environments and games with illustrate examples.
4. Demonstrate the inventory problems and EOQ models with examples.
5. Determine dynamic programming with illustrative examples and study dynamic programming models.

## UNIT I

18 hours
Integer Linear Programming - Types of Integer Programming Problems - Gomory’s All Integer Cutting Plane Method \#Gomory's Mixed Integer Cutting Plane Method\#. Sensitivity Analysis - Change in Objective Function Coefficient Addition of New Variable - Addition of New Constraint.

UNIT II

## 18 hours

Goal Programming - Difference between LP and GP approach - \#Concept of Goal Programming\# - Goal Programming model formulation - Single Goal with Multiple sub Goals - Equally ranked Multiple Goals - Ranking and Weighting of Unequal Multiple Goals - General GP Model -Graphical Solution method of GP -Modified Simplex Method of GP.

## UNIT III

## 18 hours

Decision Theory - \#Steps of Decision making process\# - Types of Decision Making Environments - Decision Making Under Uncertainty - Decision Making Under Risk - Expected Monetary Value. Theory of Games -Two Person Zero Sum Games -Games with Saddle Point -Rules to determine Saddle point -Games without Saddle Point -Related problems Principles of Dominance -Graphical Method.

## UNIT IV

## 18hours

Deterministic Inventory Control models - \#Meaning of inventory control - Reasons for carrying inventory - Factors involved in inventory problem analysis\# - Inventory cost components - Demand for inventory items - Replenishment lead time - Length of planning period - Inventory model building - Single item inventory control modes without shortages - Model I(a): EOQ model with constant rate of demand, Model I(c): Economic production Quantity model when supply is gradual. Single item inventory control models with shortages - Model II (a): EOQ model with constant rate of demand and variable order cycle time.

## UNIT V

## 18 hours

Dynamic Programming - Dynamic Programming Terminology - Developing Optimal Decision Policy - \#General Algorithm\# - Dynamic Programming Under Certainty - Model-I: Shortest Route Problem - Model-II: Multiple Separable Return Function and Single Additive Constraint -Dynamic Programming Approach for Solving Linear Programming Problems.

## Text Books:

J.K. Sharma, Operations Research Theory and Applications, Macmillan India Ltd., Fourth Edition, (2010).

UNIT I Sections 7.1, 7.2, 7.4, 7.5, 6.1 and 6.2 (6.2.1, 6.2.4, 6.2.5)
UNIT II Sections 8.1-8.6
UNIT III Sections 11.1, 11.2, 11.3, 11.4(11.4.1-11.4.5), 11.5(11.5.1) 12.1, 12.2, 12.3(12.3.1), 12.4, 12.5, 12.6.4
UNIT IV Sections 14.1, 14.2, 14.4, 14.5(14.5.1-14.5.4), 14.6(14.6.1-14.6.3), 14.7, 14.8 (Part)
UNIT V Sections 22.1, 22.2, 22.3, 22.4 (Model -I and Model -II), 22.5

## Books for Reference:

1. Prem Kumar Gupta and D.S. Hira, Operations research, S. Chand, (2000).
2. Kantiswarup, P.K. Gupta and Manmohan, Operations Research, Sultan Chand \& Sons, (2009).

## Web Source

1. https://nptel.ac.in/courses/111/107/111107128/
2. https://www.youtube.com/playlist?list=PLbMVogVj5nJT8iTaUR8FoWBuJyOvs-Z3C
3. https://www.youtube.com/channel/UCW6912n7NwIBO7rPTIxHm0w
4. https://swayam.gov.in/nd2 cec20 ma19/preview
5. https://swayam.gov.in/nd1 noc20 ma45/preview

Relationship Matrix for Course Outcomes, Programme Outcomes and Programme Specific Outcomes:


## Prepared by:

1.Dr. S. Ismail Mohideen
2. Dr. M.A. Rifayathali

Note:

| Mapping | $1-29 \%$ | $30-59 \%$ | $60-69 \%$ | $70-89 \%$ | $90-100 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Matches | $1-14$ | $15-29$ | $30-34$ | $35-44$ | $45-50$ |
| Relationship | Very poor | Poor | Moderate | High | Very high |


| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| IV | 20PMA4DE4B | DSE - IV | STOCHASTIC <br> PROCESSES | 6 | 4 | 100 | 25 | 75 |

## UNIT I

## 18 hours

Introduction - Specification of Stochastic Processes - Stationary Processes - Second- Order Processes - Stationarity Gaussian Processes - Markov Chains - Definition and examples- Transition matrix - Probability distribution - Order of a Markov chain - Markov chains as graphs - Higher transition probabilities.

## UNIT II

18 hours
Classification of States and Chains - Communication Relations - Class Property -Classifications of Chains - Classification of States: First Passage Time Distribution -Determination of Higher transition probabilities - Aperoidic Chain: Limiting Behavior - Stability of a Markov System - Limiting Behavior - \#Graph theoretic approach\#.

## UNIT III

## 18 hours

Poisson Processes - Introduction - Postulates for Poisson process - Properties of Poisson process- Poisson process and related distributions - Interarrival Time - Further Properties ofPoisson Process.

UNIT IV
18 hours
Renewal Processes - Renewal Processes in discrete time - Relation between F(s) and P(s) - Renewal interval Generalized Form: Delayed Recurrent Event - Renewal Theory in Discrete Time - Renewal Processes in Continuous Time - Renewal Function and RenewalDensity - Renewal Equation.

## UNIT V

## 18 hours

Queueing Processes - Steady State Distribution - General relationships in Queueing Theory - Little’s Formula Queueing Model M/M/1: Steady state behavior - Transient behaviour of M/M/1 Model.

## \# \# Self-study portion.

## Text Book:

Medhi, J, Stochastic Processes, Second Edition (Reprint), New Age International Publishers, New Delhi, 2002.

| UNIT I | Chapter 2 | Sections 2.1-2.3 |
| :--- | :--- | :--- |
|  | Chapter 3 | Sections 3.1, 3.2 |
| UNIT II | Chapter 3 | Sections 3.4-3.7 |
| UNIT III | Chapter 4 | Sections 4.1-4.2 |
| UNIT IV | Chapter 6 | Sections 6.1-6.3 |
| UNIT V | Chapter 10 | Sections 10.1-10.2.2, 10.3 |

## Books for Reference:

1. Basu, A. K., "Introduction to Stochastic Process", Narosa Publishing House, New Delhi, 2007.
2. Chung, K.L. and Sahlia, F.A., "Elementary Probability Theory with Stochastic Processes and an introduction to Mathematical Finance", Springer (India) Pvt. Ltd., New Delhi, 2005.
3. Srinivasan, S. K. and Mehatha, K.M., "Stochastic Processes", Tata McGraw-Hill Publishing Co. Ltd., New Delhi, 1988.

| Semester | Code | Course | Title of the <br> Course | Hours | Credits | Max. <br> marks | Internal <br> marks | External <br> marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| IV | 20PMA4EC2 | Extra Credit - II | MATHEMATICS <br> FOR CAREER <br> EXAMINATIONS | - | 5 | 100 | - | 100 |

## UNIT I

Analysis: Elementary set theory, finite, countable and uncountable sets, Real number system as a complete ordered field, Archimedean property, supremum, infimum. Sequences and series, convergence, limsup, liminf. Bolzano Weierstrass theorem, Heine Borel theorem. Continuity, uniform continuity, differentiability, mean value theorem. Sequences and series of functions, uniform convergence. Riemann sums and Riemann integral, Improper Integrals. Monotonic functions, types of discontinuity, functions of bounded variation, Lebesgue measure, Lebesgue integral. Functions of several variables, directional derivative, partial derivative, derivative as a linear transformation, inverse and implicit function theorems. Metric spaces, compactness, connectedness. Normed linear Spaces. Spaces of continuous functions as examples.
Linear Algebra: Vector spaces, subspaces, linear dependence, basis, dimension, algebra of lineartransformations. Algebra of matrices, rank and determinant of matrices, linear equations. Eigenvalues and eigenvectors, Cayley-Hamilton theorem. Matrix representation of linear transformations. Change of basis, canonical forms, diagonal forms, triangular forms, Jordan forms. Inner product spaces, orthonormal basis. Quadratic forms, reduction and classification of quadratic forms.

## UNIT II

Complex Analysis: Algebra of complex numbers, the complex plane, polynomials, power series,transcendental functions such as exponential, trigonometric and hyperbolic functions. Analytic functions, Cauchy-Riemann equations. Contour integral, Cauchy's theorem, Cauchy's integral formula, Liouville's theorem, Maximum modulus principle, Schwarz lemma, Open mapping theorem. Taylor series, Laurent series, calculus of residues. Conformal mappings, Mobius transformations.
Algebra: Permutations, combinations, pigeon-hole principle, inclusion-exclusion principle, derangements. Fundamental theorem of arithmetic, divisibility in Z, congruences, Chinese Remainder Theorem, Euler's $\varnothing$ - function, primitive roots. Groups, subgroups, normal subgroups, quotient groups, homomorphisms, cyclic groups, permutation groups, Cayley's theorem, class equations, Sylow theorems. Rings, ideals, prime and maximal ideals, quotient rings, unique factorization domain, principal ideal domain, Euclidean domain. Polynomial rings and irreducibility criteria. Fields, finite fields, field extensions, Galois Theory.
Topology: basis, dense sets, subspace and product topology, separation axioms, connectedness and compactness.

## UNIT III

## Ordinary Differential Equations (ODEs):

Existence and uniqueness of solutions of initial value problems for first order ordinary differentialequations, singular solutions of first order ODEs, system of first order ODEs. General theory of homogenous and non-homogeneous linear ODEs, variation of parameters, Sturm-Liouville boundary value problem, Green's function.

## Partial Differential Equations (PDEs):

Lagrange and Charpit methods for solving first order PDEs, Cauchy problem for first order PDEs. Classification of second order PDEs, General solution of higher order PDEs with constant coefficients, Method of separation of variables for Laplace, Heat and Wave equations.

## Numerical Analysis :

Numerical solutions of algebraic equations, Method of iteration and Newton-Raphson method, Rate of convergence, Solution of systems of linear algebraic equations using Gauss elimination and Gauss-Seidel methods, Finite differences, Lagrange, Hermite and spline interpolation, Numerical differentiation and integration, Numerical solutions of ODEs using Picard, Euler, modified Euler and Runge-Kutta methods.

## Calculus of Variations:

Variation of a functional, Euler-Lagrange equation, Necessary and sufficient conditions for extrema. Variational methods for boundary value problems in ordinary and partial differential equations.

## Linear Integral Equations:

Linear integral equation of the first and second kind of Fredholm and Volterra type, Solutions with separable kernels. Characteristic numbers and eigenfunctions, resolvent kernel.

## Classical Mechanics:

Generalized coordinates, Lagrange's equations, Hamilton's canonical equations, Hamilton's principle and principle of least action, Two-dimensional motion of rigid bodies, Euler's dynamicalequations for the motion of a rigid body about an axis, theory of small oscillations.

## UNIT IV

Descriptive statistics, exploratory data analysis Sample space, discrete probability, independent events, Bayes theorem. Random variables and distribution functions (univariate and multivariate); expectation and moments. Independent random variables, marginal and conditional distributions. Characteristic functions. Probability inequalities (Tchebyshef, Markov, Jensen). Modes of convergence, weak and strong laws of large numbers, Central Limit theorems (i.i.d. case). Markov chains with finite and countable state space, classification of states, limiting behaviour of $n$-step transition probabilities, stationary distribution, Poisson and birth-and-death processes. Standard discrete and continuous univariate distributions. sampling distributions, standard errors and asymptotic distributions, distribution of order statistics and range. Methods of estimation, properties of estimators, confidence intervals. Tests of hypotheses: most powerfuland uniformly most powerful tests, likelihood ratio tests. Analysis of discrete data and chi-square test of goodness of fit. Large sample tests. Simple nonparametric tests for one and two sample problems, rank correlation and test for independence. Elementary Bayesian inference. Gauss-Markov models, estimability of parameters, best linear unbiased estimators, confidence intervals, tests for linear hypotheses. Analysis of variance and covariance. Fixed, random and mixed effects models. Simple and multiple linear regression. Elementary regression diagnostics. Logistic regression.

## UNIT V

Multivariate normal distribution, Wishart distribution and their properties. Distribution of quadratic forms. Inference for parameters, partial and multiple correlation coefficients and related tests. Data reduction techniques: Principle component analysis, Discriminant analysis, Cluster analysis, Canonical correlation. Simple random sampling, stratified sampling and systematic sampling. Probability proportional to size sampling. Ratio and regression methods. Completely randomized designs, randomized block designs and Latin-square designs. Connectedness and orthogonality of block designs, BIBD. 2 K factorial experiments: confounding and construction. Hazard function and failure rates, censoring and life testing, series and parallel systems. Linear programming problem, simplex methods, duality. Elementary queuing and inventory models. Steady-state solutions of Markovian queuing models: $M / M / 1, M / M / 1$ with limited waiting space, M/M/C, M/M/C with limited waiting space, M/G/1.

## Text Book:

Pawan Sharma, Suraj Singh, Anshuman, UGC CSIR NET/SET (JRF \& LS) Mathematical Sciences, Arihant Publisher, 2016.

## Books for Reference:

1. CSIR-NET Toppers Handwritten Notes- Mathematical Science - 8 books- Latest Edition 2020.
2. Tripathi A. M., Truemans CSIR Mathematical Sciences , Trueman's Publisher.
3. P.C. Mittal, Ritesh Mishra, Joint CSIR UGC-NET Mathematical Sciences (Part-B \& C) Exam Guide, Ramesh Publishing House, 2020.
