## A STUDY ON APPLICATION OF FUZZY ON REAL LIFE

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## What is fuzzy

"Fuzzy" is a term used to describe something that is not clear or well defined ,often characterized by a lack of sharp boundaries or distinct categories. It can refer to a variety of concepts, such as fuzzy logic that allows for degrees of truth rather than just true or false, or it can be used in everyday language to describe something that it unclear or imprecise. Fuzziness is often associated with uncertainty and vagueness.

## Why only fuzzy

Fuzzy logic is well suited handling situations where the input data or conditions
are not crisp and well-defined. It allows for the modeling of uncertainty and vagueness, making it effective in systems with uncertain variables.

## METHOD OF OBTAINING IRDM

- By converting raw data into matrix


## ATDM

-Through dividing each irdm entry by the length of the respective category intervals

## RTDM

-Using mean and standard deviation

## CETDM

-By combining RTDMS for values of $\alpha, 0 \leq \alpha \leq 1$

## Social attributes causing divorce cases

- AT $_{1}$ - Extra Marital Relations:
- $\mathbf{A T}_{2}$ - Husband Unemployment
- $\mathrm{AT}_{3}$ - Lack of Communication
- $\mathrm{AT}_{4}$ - Arguing and Abusing
- AT $_{5}$-Quixotic Expectations
$\Rightarrow \mathbf{A T}_{\mathbf{6}}$ - Couple without Kids
- $\mathbf{A T}_{7}$ - Lack of Affinity
- $\mathbf{A T}_{\mathbf{8}}$ - Lack of Equality
- $\mathbf{A T}_{\mathbf{9}}^{\mathbf{9}}$ - Different Interests and Priorities
- $\mathbf{A T}_{10}{ }^{-}$Inability to Resolve Conflicts

Number of women responds based on their age groups

| Age -Group | Number of <br> Respondent |
| :---: | :---: |
| $18-22$ | 22 |
| $23-27$ | 22 |
| $28-32$ | 22 |
| $33-37$ | 22 |
| $38-42$ | 11 |
| $43-47$ | 11 |
|  | 110 |

IRDM of divorced women of the order $6 \times 10$

| AgeGroup | $\mathrm{AT}_{1}$ | $\mathrm{AT}_{2}$ | $\mathrm{AT}_{3}$ | $\mathrm{AT}_{4}$ | AT ${ }_{5}$ | AT 6 | AT ${ }_{7}$ | AT ${ }_{8}$ | AT ${ }_{9}$ | $\mathrm{AT}_{10}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 18-22 | 22 | 8 | 9 | 6 | 7 | 8 | 8 | 11 | 16 | 19 |
| 23-27 | 22 | 10 | 16 | 14 | 15 | 16 | 11 | 16 | 17 | 20 |
| 28-32 | 22 | 11 | 19 | 15 | 20 | 17 | 12 | 18 | 18 | 22 |
| 33-37 | 22 | 8 | 13 | 9 | 15 | 12 | 11 | 17 | 18 | 20 |
| 38-42 | 11 | 3 | 7 | 4 | 7 | 4 | 4 | 7 | 6 | 8 |
| 43-47 | 11 | 2 | 4 | 3 | 6 | 2 | 4 | 7 | 6 | 7 |


| Age- <br> Group | $\mathrm{AT}_{1}$ | $\mathrm{AT}_{2}$ | $\mathrm{AT}_{3}$ | $\mathrm{AT}_{4}$ | $\mathrm{AT}_{5}$ | $\mathrm{~A} T_{6}$ | $\mathrm{AT}_{7}$ | $\mathrm{~A} T_{8}$ | $\mathrm{~A} T_{9}$ | $\mathrm{~A} T_{10}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $18-22$ | 4.2 | 1.6 | 1.8 | 1.2 | 1.4 | 1.6 | 1.6 | 2.2 | 3.2 | 3.8 |
| $23-27$ | 4.2 | 2.0 | 3.2 | 2.82. | 3.0 | 3.2 | 2.2 | 3.2 | 3.4 | 4.0 |
| $28-32$ | 4.2 | 2.2 | 3.8 | 3.0 | 4.0 | 3.4 | 2.4 | 3.6 | 3.6 | 4.4 |
| $33-37$ | 4.2 | 1.6 | 2.6 | 1.8 | 3.0 | 2.4 | 2.2 | 3.4 | 3.6 | 4.0 |
| $38-42$ | 2.2 | 0.6 | 1.4 | 0.8 | 1.4 | 0.8 | 0.8 | 1.4 | 1.2 | 1.6 |
| $43-47$ | 2.2 | 0.4 | 0.8 | 0.6 | 1.2 | 0.4 | 0.8 | 1.4 | 1.2 | 1.4 |

Mean and Standard Deviation of the above average time dependent data matrix

| Mean | 3.53 | 1.4 | 2.26 | 1.7 | 2.33 | 1.96 | 1.66 | 2.53 | 2.7 | 3.2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Standard <br> deviation | 1.03 | 0.73 | 1.13 | 1.02 | 1.15 | 1.24 | 0.72 | 1.00 | 1.17 | 1.33 |

RTDM for $\propto=0.2$
$\left[\begin{array}{rrrrrrrrrr}1 & 1 & -1 & -1 & -1 & -1 & 0 & -1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 1 \\ -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 \\ -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1\end{array}\right]$

RTDM for $\propto=0.5$
$\left[\begin{array}{rrrrrrrrrr}1 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 0 & 0 & 0 & 1 & 0 & -1 & 1 & 1 & 1 \\ -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 \\ -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1\end{array}\right]$

Row wise sum
$\left[\begin{array}{r}-1 \\ 10 \\ 10 \\ 9 \\ -10 \\ -10\end{array}\right]$
Row wise sum
$\left[\begin{array}{r}0 \\ 10 \\ 10 \\ 4 \\ -10 \\ -10\end{array}\right]$

RTDM for $\propto=0.35$
$\left[\begin{array}{rrrrrrrrrr}1 & 0 & 0 & -1 & -1 & -1 & 0 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 0 & 0 & 0 & 1 & 1 & -1 & 1 & 1 & 1 \\ -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 \\ -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1\end{array}\right]$

RTDM for $\propto=0.65$

$$
\left[\begin{array}{rrrrrrrrrr}
1 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 \\
1 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 0 & 0 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & 0 & 0 & 0 & 0 & 0 & -1 & 1 & 1 & 0 \\
-1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 \\
-1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1
\end{array}\right]
$$

Row wise sum


Row wise sum


RTDM for $\propto=0.8$


## Row wise sum



Plotting graph for different values of alpha


Age interval of divorced women for $\propto=$ 0.2


Age interval of divorced for $\propto=0.35$


Age interval of divorced women for $\alpha=0.5$


Age interval of divorced women for $\alpha=0.65$


Age interval divorced women for $\propto=0.8$


Maximum age group of suffered women for CETDM

## FUZZY SOFT MATRIX THEORY AND ITS APPLICATION IN DECISION MAKING

## FUZZY SOFT MATRICES

Fs- matrices which are representations of the fs- sets. This style of representation is useful for storing a soft set in a computer memory. The operations can be presented by the matrices which are very useful and convenient for the application.

A set off all fuzzy sets over $U$ will be denoted by $F(U)$. ГА, гв, гс, ..., etc. and $\gamma \mathrm{A}, \gamma \mathrm{B}, \gamma \mathrm{C}, \ldots$. , etc. will be used for fs- sets and their fuzzy approximate functions, respectively.

$$
\Gamma_{A}: E \rightarrow F(U) \text { such that } \gamma_{A}(x)=\varnothing \text { if } x \in / A
$$

Here, $\gamma_{A}$ is called fuzzy approximate function of the fs-set $\Gamma_{A}$, the value $\gamma_{A}(x)$ is a fuzzy set called $x$-element of the fs-set for all $x \in E$, and $\varnothing$ is the null fuzzy set. Thus, an fs-set $\Gamma_{A}$ over $U$ can be represented by the set of ordered pairs

$$
\Gamma_{A}=\left\{\left(x, \gamma_{A}(x)\right): x \in E, \gamma_{A}(x) \in F(U)\right\} .
$$

The sets of all fs-sets over U will be denoted by F S(U).

* A zero fs-matrix, denoted by [0].
* An A-universal fs-matrix, denoted by $\left[a_{\mathrm{ij}}\right]$.
* A universal fs-matrix, denoted by [1].
* Union of $\left[a_{i j}\right]$ and $\left[b_{i j}\right]$, denoted $\left[a_{i j}\right] \widetilde{\cup}\left[b_{i j}\right]$, if $c_{i j}=\max \left\{a_{i j}, b_{i j}\right\}$.
* Intersection of $\left[\mathrm{a}_{\mathrm{ij}}\right]$ and $\left[\mathrm{b}_{\mathrm{ij}}\right]$, denoted $\left[\mathrm{a}_{\mathrm{ij}}\right] \widetilde{n}\left[\mathrm{~b}_{\mathrm{ij}}\right]$, if $\mathrm{c}_{\mathrm{ij}}=\min \left\{a_{i j}, \mathrm{~b}_{\mathrm{ij}}\right\}$.
* Complement of $\left[a_{i j}\right]$, denoted by $\left[a_{i j}\right]^{\circ}$, if $\mathrm{c}_{\mathrm{ij}}=1-\mathrm{a}_{\mathrm{ij}}$.

$$
\begin{aligned}
& *\left[a_{i j}\right] \widetilde{n}\left[b_{i j}\right]=\left[b_{i j}\right] \widetilde{n}\left[a_{i j}\right] \\
& *\left[a_{i j}\right] \widetilde{U}\left[b_{i j}\right]=\left[b_{i j}\right] \widetilde{U}\left[a_{i j}\right] \\
& *\left[a_{i j}\right] \widetilde{n}\left[a_{i j}\right]^{\circ}=[0] \\
& *\left[a_{i j}\right] \widetilde{U}\left[a_{i j}\right]^{\circ}=[1]
\end{aligned}
$$

PRODUCTS OF fs- MATRICESAnd-Product

$$
\begin{aligned}
& \wedge: \mathrm{FSM}_{\mathrm{mxn}} \times \mathrm{FSM}_{\mathrm{mxn}} \rightarrow \mathrm{FSM}_{\mathrm{mxn2}},\left[\mathrm{a}_{\mathrm{ij}}\right] \wedge\left[\mathrm{b}_{\mathrm{ik}}\right]=\left[\mathrm{c}_{\mathrm{ip}}\right] \\
& \text { where }, \mathrm{c}_{\mathrm{ip}}=\min \left\{\mathrm{a}_{\mathrm{ij}}, \mathrm{~b}_{\mathrm{ik}}\right\} \text { such that } \mathrm{p}=\mathrm{n}(\mathrm{j}-1)+\mathrm{k} .
\end{aligned}
$$Or- Product

$$
V: \mathrm{FSM}_{m \times n} \times \mathrm{FSM}_{m \times n} \rightarrow \mathrm{FSM}_{m \times n 2},\left[\mathrm{a}_{\mathrm{ij}}\right] \vee\left[\mathrm{b}_{\mathrm{ik}}\right]=\left[\mathrm{c}_{\mathrm{ip}}\right]
$$

Where, $\mathrm{c}_{\mathrm{ip}}=\max \left\{\mathrm{a}_{\mathrm{ij}}, \mathrm{b}_{\mathrm{ik}}\right\}$ such that $\mathrm{p}=\mathrm{n}(\mathrm{j}-1)+\mathrm{k}$.And-Or Product
Z: $\mathrm{FSM}_{\text {mxn }} \times \mathrm{FSM}_{\text {mxn }} \rightarrow \mathrm{FSM}_{\text {mxn2 }},\left[\mathrm{a}_{\mathrm{ij}}\right] \mathrm{Z}\left[\mathrm{b}_{\mathrm{ik}}\right]=\left[\mathrm{c}_{\mathrm{ip}}\right]$
where,$c_{i p}=\min \left\{a_{i j}, 1-b_{i k}\right\}$ such that $p=n(j-1)+k$.Or-Not Product

$$
\mathrm{Y}: \mathrm{FSM}_{m \times n} \times \mathrm{FSM}_{m \times n} \rightarrow \mathrm{FSM} M_{m \times n 2},\left[\mathrm{a}_{\mathrm{ij}}\right] \mathrm{Y}\left[\mathrm{~b}_{\mathrm{ik}}\right]=\left[\mathrm{c}_{\mathrm{ip}}\right]
$$

where, $c_{i p}=\max \left\{a_{i j}, 1-b_{i k}\right\}$ such that $p=n(j-1)+k$.

## fs-Max-Min DECISION MAKING

$$
\left.M m: \mathrm{FSM}_{\mathrm{mxn} \mathrm{\times 2}} \rightarrow \mathrm{FSM}_{\mathrm{mx} 1}, \mathrm{Mm}\left[\mathrm{c}_{\mathrm{ip}}\right]=\left[\mathrm{d}_{\mathrm{i} 1}\right]=\max _{\mathrm{k}}\left\{\mathrm{t}_{\mathrm{ik}}\right\}\right]
$$

Let $U=\left\{u_{1}, u_{2}, \ldots, u_{m}\right\}$ be an initial universe and $M m\left[c_{i p}\right]=\left[d_{i 1}\right]$.
Then a subset of $U$ can be obtained by using $\left[d_{i 1}\right]$ as in the following way

$$
\operatorname{opt}\left[d_{i 1}\right](U)=\left\{d_{i 1} / u_{i}: u_{i} \in U, d_{i 1}=0\right\}
$$

which is called an optimum fuzzy set on $U$.
Now, using definitions we can construct a FSMmDM method by the following algorithm.

Now, using definitions we can construct a FSMmDM method by the following algorithm.

Step 1: choose feasible subsets of the set of parameters,
Step 2: construct the fs-matrix for each set of parameters,
Step 3: find a convenient product of the fs-matrices,
Step 4: find a max-min decision fs-matrix,
Step 5: find an optimum fuzzy set on U.
We can define fs-min-max, fs-min-min and fs-max-max decision-making methods
which may be denoted by (FSmMDM), (FSmmDM), (FSMMDM), respectively.

## REAL APPLICATION

Suppose the laptop trader has a laptop of unlike companies $G=\left\{g_{1}, g_{2}, g_{3}, g_{4}, g_{5}\right\}$. They can be categorized by a set of parameters $Z=\left\{z_{1}, z_{2}, z_{3}, z_{4}\right\}$. Here $j=1,2,3,4$ the constraints signify "Processor Speed", "Battery Backup", "Price" and "RAM/ROM" respectively

## Example

Assume that two users reach at the shop of laptop trader to get laptop. Each user selects parameters according to their choice, now we choose a laptop with the help of FSMmDM depends on the sets of user's parameters.

Let $G=\left\{g_{1}, g_{2}, g_{3}, g_{4}, g_{5}\right\}$ is a universal set and $Z=\left\{z_{1}, z_{2}, z_{3}, z_{4}\right\}$ collection of constraints.

Phase 1: User first, user second will select the collection of constraints according to their choice, $P=\left\{z_{2}, z_{3}, z_{4}\right\}$ and $Q=\left\{z_{1}, z_{3}, z_{4}\right\}$, one-to-one

Phase 2: Now we compose these two FS-matrices with the help of bar diagram, these are based on user's parameters


Processer Speed


Price


Battery Performance


RAM/ROM
Phase 3: These two FS-matrices $\left[\mathrm{x}_{\mathrm{ij}}\right]$ and $\left[\eta_{\mathrm{ik}}\right]$ can multiply with the help of And Product

$$
\left[\chi_{i j}\right]=\left[\begin{array}{cccc}
0 & 0.8 & 0.5 & 1 \\
0 & 0.2 & 0.4 & 0.8 \\
0 & 0.8 & 1 & 1 \\
0 & 1 & 0.3 & 1 \\
0 & 0.8 & 0.8 & 1
\end{array}\right] \quad\left[\eta_{i \mathrm{ik}}\right]=\left[\begin{array}{cccc}
1 & 0 & 0.5 & 1 \\
0.6 & 0 & 0.4 & 0.8 \\
0.5 & 0 & 1 & 1 \\
0.8 & 0 & 0.3 & 1 \\
0.7 & 0 & 0.8 & 1
\end{array}\right]
$$

$$
\left[\begin{array}{cccccccccccccccc}
0 & 0 & 0 & 0 & 0.8 & 0 & 0.5 & 0.8 & 0.5 & 0 & 0.5 & 0.5 & 1 & 0 & 0.5 & 1 \\
0 & 0 & 0 & 0 & 0.2 & 0 & 0.2 & 0.2 & 0.4 & 0 & 0.4 & 0.4 & 0.6 & 0 & 0.4 & 0.8 \\
0 & 0 & 0 & 0 & 0.5 & 0 & 0.8 & 0.8 & 0.5 & 0 & 1 & 1 & 0.5 & 0 & 1 & 1 \\
0 & 0 & 0 & 0 & 0.8 & 0 & 0.3 & 1 & 0.3 & 0 & 0.3 & 0.3 & 0.8 & 0 & 0.3 & 1 \\
0 & 0 & 0 & 0 & 0.7 & 0 & 0.8 & 0.8 & 0.7 & 0 & 0.8 & 0.8 & 0.7 & 0 & 0.8 & 1
\end{array}\right]
$$

Phase 4: We solve $M m\left(\left[\mathrm{X}_{\mathrm{ij}}\right]\left[\eta_{\mathrm{ik}}\right]\right)=[$ di11], and get di1 for every $\mathrm{i}\{1,2,3,4,5\}$. Calculate $\mathrm{d}_{11}$.

Subsequently $\mathrm{i}=1, \mathrm{k}\{1,2,3,4\}$.

$$
\mathrm{d}_{11}=\max \mathrm{k}\{\mathrm{t} 1 \mathrm{k}\}=\max \left\{\mathrm{t}_{11}, \mathrm{t}_{12}, \mathrm{t}_{13}, \mathrm{t}_{14}\right\}
$$

In this phase, we have to find t 1 k for all $\mathrm{k}\{1,2,3,4\}$. To determine, Now we calculate $\mathrm{t}_{11}$ and $\mathrm{t} 12 . \mathrm{I} 1=\left\{\mathrm{s}: \mathrm{c}_{\mathrm{is}} \neq 0,0<\mathrm{s} 4\right\}=\varphi$; for $\mathrm{k}=1$ and $\mathrm{n}=4$ and
$I 2=\left\{s: c_{\text {is }} \neq 0 ; 4<\mathrm{s} 8\right\}=\{5,7,8\}$ on behalf of $k=2, n=4$, Here after $t_{11}=0$

$$
\mathrm{T}_{12}=\min \left\{\mathrm{c}_{15}, \mathrm{c}_{17}, \mathrm{c}_{18}\right\}=\min \{0.8,0.5,0.8\}=0.5
$$

Similarly, we calculate as $\mathrm{t}_{13}=0.5$ and $\mathrm{t}_{14}=0.5$. Then.

$$
d_{11}=\max \{0.0,0.5,0.5,0.5\}=0.5
$$

$$
\operatorname{Mm}\left(\left(x_{i j}\right)^{\wedge}\left[n_{i . k}\right)=\left[\mathrm{d}_{\mathrm{i}}\right]=\left[\begin{array}{c}
0.5 \\
0.4 \\
0.5 \\
0.3 \\
0.3
\end{array}\right]\right.
$$

Similarly, we calculate $d_{21}=0.4, d_{31}=0.5, d_{41}=0.3$ and $d_{51}=0.7$. In the end, got the FS-max-min judgment fuzzy soft matrix in the form of one column.

Phase 5: At Last, Mm ( $\left.\left[\mathrm{x}_{\mathrm{ij}}\right]\left[\eta_{\mathrm{ik}}\right]\right)$ permit us to calculate a finest fuzzy set on $G$.
$(G)=\left\{0.5 / \mathrm{g}_{1}, 0.7 / \mathrm{g}_{5}\right\}$.
Here $g_{5}$ is a best laptop to purchase for user first and user second according to their desires. In the same way, for any appropriate problems apply these products

## An Adjustable Approach of FSMmDM Method in Automobile

## Preliminaries

In the beginning, fuzzy soft matrices is given by fuzzy soft set here. This type technique is very useful for creating matrices as well as operating it in computer memory. Now, we show (H) as a group of every fuzzy set for H .

We show $\pi \alpha, \pi \beta, \pi \gamma, \ldots$, etc. as fuzzy soft sets and $r \alpha, r \beta, r \gamma, \ldots$, etc. show as a fuzzy predicted task of their fuzzy soft sets. H signify elementary universe here, S signifies assemblage of specification, $\alpha \in \mathrm{S}, r(t) * \mathrm{t} \in \mathrm{S}$. Here fuzzy soft set $\pi \alpha$ for H . Keep in your mind, FS $(\mathrm{H})$ signifies assemblage of every FS-set for H .

## Sample

Now alliance structure of $\pi \alpha$ shown below.
We use the concept of 3.2.1.2.

$$
T \alpha=\left\{0.9 /\left(\mathrm{CR}_{1}, \mathrm{t}_{2}\right), 0.5 /\left(\mathrm{CR}_{2}, \mathrm{t}_{2}\right), 0.6 /\left(\mathrm{CR}_{3}, \mathrm{t}_{2}\right), 1 /\left(\mathrm{CR}_{4}, \mathrm{t}_{2}\right), 0.7 /\left(\mathrm{CR}_{5}, \mathrm{t}_{2}\right),\right.
$$

$\left.0.8 /\left(\mathrm{CR}_{1}, \mathrm{t}_{3}\right), 0.1 /\left(\mathrm{CR}_{2}, \mathrm{t}_{3}\right), 0.5 /\left(\mathrm{CR}_{3}, \mathrm{t}_{3}\right), 1 /\left(\mathrm{CR}_{4}, \mathrm{t}_{3}\right)\right\}$
FS-matrix $\left[K_{a b}\right.$ ] shown below.

$$
\left[\mathrm{k}_{\mathrm{ab}}\right]=\left[\begin{array}{cccc}
0 & 0.9 & 0.8 & 0 \\
0 & 0.5 & 0.1 & 0 \\
0 & 0.6 & 0.5 & 0 \\
0 & 1 & 1 & 0 \\
0 & 0.7 & 0 & 0
\end{array}\right]
$$

## MEASURES OF FUZZINESS

It is function from power set $\mathrm{P}(\mathrm{X})$ to $[0,+\infty] . \tilde{A}$ is fuzzy set, $\mu_{\tilde{A}}(\mathrm{x})$ its membership function. Measure of fuzziness d ( $\tilde{A}$ ) satisfies these properties.

1) $\mathrm{d}(\tilde{A})=0$ if $\tilde{A}$ is a crisp set in X .
2) $\mathrm{d}(\tilde{A})$ is maximum if $\mu_{\tilde{A}}(\mathrm{x})=\frac{1}{2} \quad \forall \mathrm{x} \in \mathrm{X}$,
3) $\mathrm{d}(\tilde{A}) \geq \mathrm{d}\left(\tilde{A}^{\prime}\right)$

## FS-MAX-MIN SELECTION BUILDING APPROACH

Now, we get FS-max-min selection building (FSMmDM) approach to follow FS- max-min selection task.

## APPLICATIONS

The owner of car agency have five different car signifies by $\mathrm{H}=\left\{\mathrm{CR}_{1}, \mathrm{CR}_{2}\right.$, $\left.\mathrm{CR}_{3}, \mathrm{CR}_{4}, \mathrm{CR}_{5}\right\}$. These cars are classified by the group of specification $\mathrm{S}=\left\{\mathrm{t}_{1}, \mathrm{t}_{2}\right.$, $\left.t_{3}, t_{4}\right\}$.

Now $\mathrm{b}=1,2,3,4$ the specification tb indicates high "CC (cubic centimeter capacity of combustion cylinder)", best "Average", "Cheap Price" and "Goodlooking" respectively. We will solve this example

Husband and wife, reach at the car agency for purchasing car. Each partner preferred specification according their desire. We will buy car depend on the group of partners specification by using FSMmDM as shown below. Suppose $H=\left\{\mathrm{CR}_{1}, \mathrm{CR}_{2}, \mathrm{CR}_{3}, \mathrm{CR}_{4}, \mathrm{CR}_{5}\right\}$ signifies universal set and $\mathrm{S}=\left\{\mathrm{t}_{1}, \mathrm{t}_{2}, \mathrm{t}_{3}, \mathrm{t}_{4}\right\}$ group of specification.

Phase 1: Husband and wife likes this type of group of specification, $\mathrm{P}=$ $\left\{\mathrm{t}_{1}, \mathrm{t}_{3}, \mathrm{t}_{4}\right\}$ and $\mathrm{B}=\left\{\mathrm{t}_{2}, \mathrm{t}_{3}, \mathrm{t}_{4}\right\}$.

Phase 2: Two FS-matrices are given, these have been established on specification. We get the mileage in cubic centimeter (CC) of all cars and assign membership value in figure 4.1


Fig: 4.1: Membership Value According To Their CC

We get the average in kilometer per hour ( $\mathrm{Km} / \mathrm{h}$ ) of all cars and assign membership value in figure 4.2.2


Fig: 4.2: Membership Value According To Their Average
We get the price of all cars in lacks and assign membership value in figure 4.3.


Fig: 4.3: Membership Value According To Their Price

We see the body structure and all function of all cars and assign membership value in figure 4.4.


Fig: 4.4: Membership Value According To Their Good Look
Compose these two FS-matrices based on user first, user second choice in phase 1 and have taken the help of above bar diagram
$\left[\mathrm{k}_{\mathrm{ab}}\right]=\left[\begin{array}{cccc}0.7 & 0 & 0.8 & 0.4 \\ 1 & 0 & 0.2 & 0.8 \\ 0.8 & 0 & 0.5 & 0.7 \\ 0.5 & 0 & 1 & 1 \\ 0.6 & 0 & 0.1 & 0.1\end{array}\right] \quad\left[\mathrm{m}_{\mathrm{ac}}\right]=\left[\begin{array}{cccc}0 & 0.9 & 0.8 & 0.4 \\ 0 & 0.5 & 0.2 & 0.8 \\ 0 & 0.6 & 0.5 & 0.7 \\ 0 & 1 & 1 & 1 \\ 0 & 0.7 & 0.1 & 0.1\end{array}\right]$

Phase 3: Apply And-product on FS -matrices $\left[\mathrm{k}_{\mathrm{ab}}\right]$ and $\left[\mathrm{m}_{\mathrm{ac}}\right]$, as shown below

$$
\left[\begin{array}{cccccccccccccccc}
0 & 0.7 & 0.7 & 0.4 & 0 & 0 & 0 & 0 & 0 & 0.8 & 0.8 & 0.4 & 0 & 0.4 & 0.4 & 0.4 \\
0 & 0.5 & 0.2 & 0.8 & 0 & 0 & 0 & 0 & 0 & 0.2 & 0.2 & 0.2 & 0 & 0.5 & 0.2 & 0.8 \\
0 & 0.6 & 0.5 & 0.7 & 0 & 0 & 0 & 0 & 0 & 0.5 & 0.5 & 0.5 & 0 & 0.6 & 0.5 & 0.7 \\
0 & 0.5 & 0.5 & 0.5 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 \\
0 & 0.6 & 0.1 & 0.1 & 0 & 0 & 0 & 0 & 0 & 0.1 & 0.1 & 0.1 & 0 & 0.1 & 0.1 & 0.1
\end{array}\right]
$$

Above, Apply And-product, for studying Husband and wife's selections.

## A GENERALISED REAL-LIFE PROBLEM SOLVED BY UNI INT DECISION MAKING METHOD

Preliminaries

* Universal set-T
* Parameter set -H
* Power set of T-P(T)


## Definition

The ordered pair of soft set $\mathrm{F}_{\mathrm{P} 1}$ over T is describing below.

$$
\mathrm{F}_{\mathrm{p} 1}=\left\{\left(\mathrm{h}, \mathrm{f}_{\mathrm{p} 1}(\mathrm{~h})\right): \mathrm{h} \in H, \mathrm{f}_{\mathrm{p} 1}(\mathrm{~h}) \in \mathrm{P}(\mathrm{~T})\right\},
$$

Here $f_{P 1}: H \rightarrow P(T), F_{p 1}(h)=\emptyset$ if $h \in P_{1}$.

Now, the fuzzy approximation function of $\mathrm{F}_{\mathrm{p} 1}$ is denoted by $f_{p 1}$. The soft set can be obtained by solving $f_{p 1}(h)$ and these are h-element of set. It is very important to remember that $f_{p 1}(h)$ may or may not give any arbitrary values. Thus, we will denote $C(T)$ as a collection of soft set for $T$. Below examples show that above theory works properly

## Example

$\mathrm{F}_{\mathrm{P} 1}$ is soft set and tells the desire of students who wants to take rent room near their university. Let us assume that six rooms are available near to university on rent $T=\left\{t_{1}, t_{2}, t_{3}, t_{4}, t_{5}, t_{6}\right\}$ and $H=\left\{h_{1}, h_{2}, h_{3}, h_{4}, h_{5}\right\}$ indicates the collection of parameters. The parameters hi $(1,2,3,4,5)$ shows as "Low Rent", "Near Institute", "Good Locality", "Accommodation Type", "Security" respectively. Hence, we select "Near Institute", "Accommodation Type", "Security" as soft set. Suppose, $P_{1}=\left\{h_{2}, h_{4}, h_{5}\right\} \subseteq H$ and $f_{p 1}\left(h_{2}\right)=\left\{\mathrm{t}_{5}, \mathrm{t}_{6}\right\}, \mathrm{f}_{\mathrm{p} 1}\left(\mathrm{~h}_{4}\right)=\left\{\mathrm{t}_{1}, \mathrm{t}_{2}, \mathrm{t}_{3}\right\}$ and $\mathrm{f}_{\mathrm{p} 1}\left(\mathrm{~h}_{5}\right)=\mathrm{T}$.

Hence, the soft set $F_{p 1}$ as a set of order pairs define below

$$
F_{p 1}=\left\{\left(h_{2},\left\{t_{5}, t_{6}\right\}\right),\left(h_{4},\left\{t_{1}, t_{2}, t_{3}\right\}\right),\left(h_{5}, \mathrm{~T}\right)\right\}
$$

## UNI-INT JUDGEMENT BUILDING METHOD

Here, a Uni-int approach is built by $\wedge$-product, $\wedge$-product is built by the combination of Uni-int operators and Uni-int judgment function. On behalf of requirement of decision maker this process diminishes a set of its subset. So decision maker takes less number of requirements not more requirement. In this section, suppose $\wedge(T)$ indicates the collection of all $\wedge$-product of soft set over T .

Rule 1 : Take beneficial subsets from a group of attributes.

Rule 2: Make the soft sets for every group of' attributes.

Rule 3: Obtain the multiplication of two soft sets.

Rule 4: Calculate the Uni-int judgment set for above And operation.

In the end, we get Uni-int decision set. By this method we obtain subset of the decision set. In the end we take a general problem and solve by Uni-int decision method.

## Example

Suppose two friends (Ram and Shyam) want to take rent room who are studying in the same university. They met many brokers who showed total number of 45 rent rooms with different parameters in different location. Ram and Syam is decision maker here. They wish to choose any one rent room. It is a difficult task. So we use this method for decreasing the collection of rent room.

Suppose $T=\left\{\mathrm{t}_{1}, \mathrm{t}_{2}, \mathrm{t}_{3}, \ldots \ldots . . \mathrm{t}_{45}\right\}$ is the set of rent room. These rent rooms have different attributes as indicated by this set $H=\left\{h_{1}, h_{2}, h_{3}, \ldots . . . h_{6}\right\}$. Here $i=1,2,3 . \ldots . .6, h_{i}$ indicates "Low Rent", "Near Institute", "Good Locality", "Accommodation Type", "Security", "Transport Facilities" respectively.

So we solve above problem by Uni-Int decision making method.

Rule 1: $P_{1}=\left\{h_{3}, h_{4}, h_{5}, h_{6}\right\}, P_{2}=\left\{h_{2}, h_{4}, h_{6}\right\}$, these are the parameters(requirement) of decision maker(Ram and Syam) according to these parameters they want to choose a rent room.

Rule 2: Ram and Shyam sincerely see the facilities of all rent room. After seeing, every rent room is check according to own required attributes. $\mathrm{P}_{1}, \mathrm{P}_{2} \underline{C}$ H, Ram and Shyam calculate two soft set according to their requirement which are given below


Rule 3: We calculate And-product ( $\left(\mathrm{Fp} 1 \wedge \mathrm{~F}_{\mathrm{p} 2}\right)$ of above soft sets.

$$
\begin{aligned}
& \left(\left(h_{3}, h_{2}\right),\left(t_{3}, t_{20}, t_{27}, t_{40}, t_{43}\right)\right. \text {, } \\
& \left.\left(h_{3}, h_{4}\right),\left(t_{12}, t_{31}, t_{35}, t_{44}\right)\right\} \text {, } \\
& \left(\left(h_{3}, h_{6}\right),\left\{t_{3}, t_{27}, t_{44}\right\}\right) \text {, } \\
& \left(\left(h_{4}, h_{2}\right),\left(t_{2}, t_{4}, t_{2}, t_{27}, t_{43}, t_{4},\right\}\right) \text {, } \\
& \left.\left(h_{4}, h_{4}\right),\left\{t_{2}, t_{12}, t_{21}, t_{31}, t_{3}, t_{45}\right\}\right) \text {, } \\
& \left.\left(h_{4}, h_{6}\right),\left(t_{4}, t_{18}, t_{21}, t_{23}, t_{27}, t_{45}\right)\right) \text {, } \\
& \text { ((h) } \left.\left., h_{2}\right),\left(t_{2}, t_{14}, t_{22}, t_{27}, t_{32}\right)\right) \text {, } \\
& \left(\left(h_{5}, h_{4}\right),\left(t_{2}, t_{12}, t_{14}, t_{29}, t_{32}, t_{3} 5\right)\right. \text { ), } \\
& \text { ( } \left.h_{5}, h_{6} \text { ), }\left\{t_{14}, t_{27}\right\}\right) \text {, } \\
& \left(\left(h_{6}, h_{2}\right),\left(t_{2}, t_{4}, t_{2}, t_{33}, t_{40}, t_{4}\right)\right) \text {, } \\
& \text { ( }\left(h_{6}, h_{4}\right),\left(t_{2}, t_{11}, t_{12}, t_{35}, t_{44}, t_{4}\right) \text { ), } \\
& \left(h_{6}, h_{6}\right),\left(t_{4}, t_{11}, t_{23}, t_{27}, t_{44}, t_{45}\right) \text {, }
\end{aligned}
$$

Rule 4: So, in the end we calculate $\operatorname{Uni}_{x}-\operatorname{lnt}_{y}\left(F_{p 1} \wedge F_{p 2}\right)$ and $\operatorname{Uni}_{y}-\operatorname{lnt}_{x}\left(F_{p 1} \wedge \mathcal{F}_{\mathrm{p} 2}\right)$ in this form

$$
U_{n i}-\operatorname{lnt} y_{y}(F p 1 \wedge F p 2)=
$$

Rule 4: So, in the end we calculate $\operatorname{Uni}_{x}-\operatorname{Int}_{y}\left(F_{p 1} \wedge F_{p 2}\right)$ and $\operatorname{Uni}_{y}-\operatorname{Int}_{x}\left(F_{p 1} \wedge F_{p 2}\right)$ in this form

$$
\text { Uni }_{x}-\text { Int }_{y}(\mathrm{Fp} 1 \wedge F p 2)=
$$

$\cap\left\{\left\{\mathrm{t}_{3}, \mathrm{t}_{20}, \mathrm{t}_{27}, \mathrm{t}_{40}, \mathrm{t}_{43}\right\},\left\{\mathrm{t}_{12}, \mathrm{t}_{31}, \mathrm{t}_{35}, \mathrm{t}_{44}\right\},\left\{\mathrm{t}_{3}, \mathrm{t}_{27}, \mathrm{t}_{44}\right\}\right\}$,
$\cap\left\{\left\{\mathrm{t}_{2}, \mathrm{t}_{4}, \mathrm{t}_{20}, \mathrm{t}_{27}, \mathrm{t}_{43}, \mathrm{t}_{45}\right\},\left\{\mathrm{t}_{2}, \mathrm{t}_{12}, \mathrm{t}_{21}, \mathrm{t}_{31}, \mathrm{t}_{35}, \mathrm{t}_{45}\right\},\left\{\mathrm{t}_{4}, \mathrm{t}_{18}, \mathrm{t}_{21}, \mathrm{t}_{23}, \mathrm{t}_{27}, \mathrm{t}_{4}\right\}\right\}$,
$\cap\left\{\left\{\mathrm{t}_{2}, \mathrm{t}_{14}, \mathrm{t}_{22}, \mathrm{t}_{27}, \mathrm{t}_{32}\right\},\left\{\mathrm{t}_{2}, \mathrm{t}_{12}, \mathrm{t}_{14}, \mathrm{t}_{29}, \mathrm{t}_{32}, \mathrm{t}_{35}\right\},\left\{\mathrm{t}_{14}, \mathrm{t}_{27}\right\}\right\}$,
$\cap\left\{\left\{\mathrm{t}_{2}, \mathrm{t}_{4}, \mathrm{t}_{27}, \mathrm{t}_{33}, \mathrm{t}_{40}, \mathrm{t}_{45}\right\},\left\{\mathrm{t}_{2}, \mathrm{t}_{11}, \mathrm{t}_{12}, \mathrm{t}_{35}, \mathrm{t}_{44}, \mathrm{t}_{45}\right\},\left\{\mathrm{t}_{4}, \mathrm{t}_{11}, \mathrm{t}_{23}, \mathrm{t}_{27}, \mathrm{t}_{44}, \mathrm{t}_{45}\right\}\right\}$,
$=u\left\{\varnothing,\left\{\mathrm{t}_{45}\right\},\left\{\mathrm{t}_{14}\right\},\left\{\mathrm{t}_{45}\right\}\right\}=\left\{\mathrm{t}_{14}, \mathrm{t}_{45}\right\}$

$$
\text { Uni } \left._{y}-\operatorname{lnt}_{x}(F p 1 \wedge F p 2)=\right)=
$$

$$
\begin{aligned}
& \cap\left\{\left\{\mathrm{t}_{3}, \mathrm{t}_{20}, \mathrm{t}_{27}, \mathrm{t}_{40}, \mathrm{t}_{43}\right\},\left\{\mathrm{t}_{2}, \mathrm{t}_{4}, \mathrm{t}_{20}, \mathrm{t}_{27}, \mathrm{t}_{43}, \mathrm{t}_{45}\right\},\left\{\mathrm{t}_{2}, \mathrm{t}_{14}, \mathrm{t}_{22}, \mathrm{t}_{27}, \mathrm{t}_{32}\right\},\right. \\
& \left.\left\{\mathrm{t}_{2}, \mathrm{t}_{4}, \mathrm{t}_{27}, \mathrm{t}_{33}, \mathrm{t}_{40}, \mathrm{t}_{45}\right\}\right\} \text {, } \\
& \cap\left\{\left\{\mathrm{t}_{12}, \mathrm{t}_{31}, \mathrm{t}_{35}, \mathrm{t}_{27}, \mathrm{t}_{44}\right\},\left\{\mathrm{t}_{2}, \mathrm{t}_{12}, \mathrm{t}_{21}, \mathrm{t}_{31}, \mathrm{t}_{35}, \mathrm{t}_{45}\right\},\left\{\mathrm{t}_{2}, \mathrm{t}_{12}, \mathrm{t}_{14}, \mathrm{t}_{29}, \mathrm{t}_{32}, \mathrm{t}_{35}\right\}\right\} \text {, } \\
& \left.\left\{\mathrm{t}_{2}, \mathrm{t}_{11}, \mathrm{t}_{12}, \mathrm{t}_{35}, \mathrm{t}_{44}, \mathrm{t}_{45}\right\}\right\} \text {, } \\
& \cap\left\{\left\{\mathrm{t}_{3}, \mathrm{t}_{27}, \mathrm{t}_{44}\right\},\left\{\mathrm{t}_{4}, \mathrm{t}_{18}, \mathrm{t}_{21}, \mathrm{t}_{23}, \mathrm{t}_{27}, \mathrm{t}_{45}\right\},\left\{\mathrm{t}_{14}, \mathrm{t}_{27}\right\}\right\}, \\
& \left.\left\{\mathrm{t}_{4}, \mathrm{t}_{11}, \mathrm{t}_{23}, \mathrm{t}_{27}, \mathrm{t}_{44}, \mathrm{t}_{45}\right\}\right\} \text {, } \\
& =\mathrm{u}\left\{\left\{\mathrm{t}_{27}\right\},\left\{\mathrm{t}_{12}, \mathrm{t}_{35}\right\},\left\{\mathrm{t}_{27}\right\}\right\}=\left\{\mathrm{t}_{12}, \mathrm{t}_{27}, \mathrm{t}_{35}\right\}
\end{aligned}
$$

Now, Ram and Shyam Can take any one rent room which is the element of Uni-Int Decision set.
$\operatorname{Uni}-\operatorname{Int}\left(F_{p 1} \wedge F_{p 2}\right)=\operatorname{Uni}_{x}-\operatorname{Int}_{y}\left(F_{p 1} \wedge F_{p 2}\right) \quad \operatorname{Uni}_{y}-\operatorname{Int}_{x}\left(F_{p 1} \wedge F_{p 2}\right)$.

$$
=\left\{\mathrm{t}_{14}, \mathrm{t}_{45}\right\} \cup\left\{\mathrm{t}_{12}, \mathrm{t}_{27}, \mathrm{t}_{35}\right\}=\left\{\mathrm{t}_{12}, \mathrm{t}_{14}, \mathrm{t}_{27}, \mathrm{t}_{35}, \mathrm{t}_{45}\right\} .
$$

## Conclusion

$\checkmark \quad$ The divorces problem using fuzzy matrix method purpose is to find out the age interval of women affected by divorces problem .
$\checkmark$ Fuzzy soft matrices in decision making method is provided an application for users to select a best laptop .
$\checkmark$ An adjustable approach of FSM and DM method having the utilization in the field of automobile for buying car.
$\checkmark$ Uni-Int decision making method is help to reduce the parameters like above room rent problem. Uni-Int method gives best results than other methods .

